

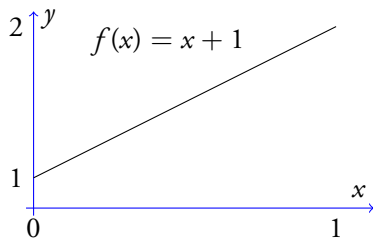
Integral med trappstegfunktioner



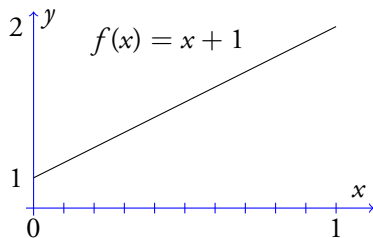
Integral med trappstegfunktioner



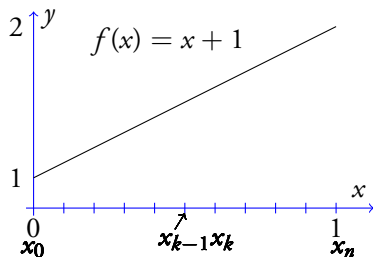
Integral med trappstegfunktioner



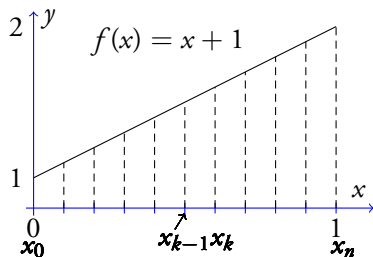
Integral med trappstegfunktioner



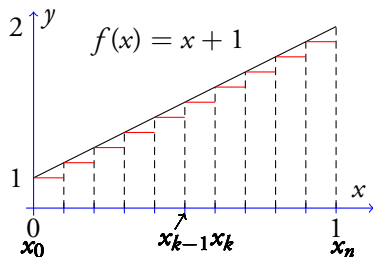
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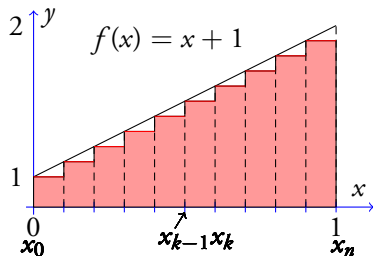
Integral med trappstegfunktioner



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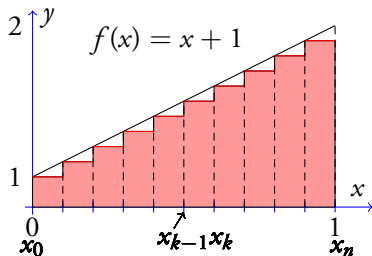
Integral med trappstegfunktioner



$$\int_0^1 \Phi_n(x) dx = \sum_{k=1}^n f(x_{k-1})(x_k - x_{k-1}) =$$



Integral med trappstegfunktioner

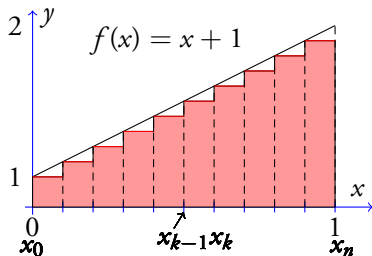


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Integral med trappstegfunktioner

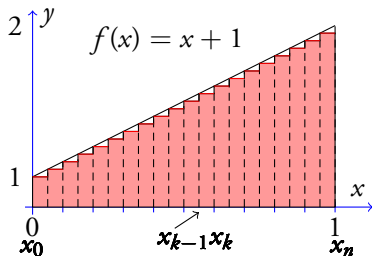


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$$= \frac{1}{2} \frac{n(n+1)}{n^2} + 1 - \frac{1}{n}$$



Integral med trappstegfunktioner

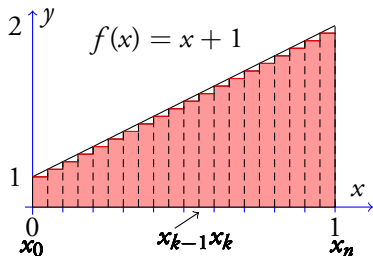


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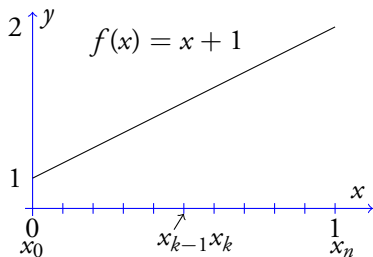
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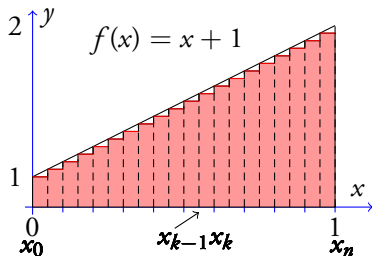
Integral med trappstegfunktioner



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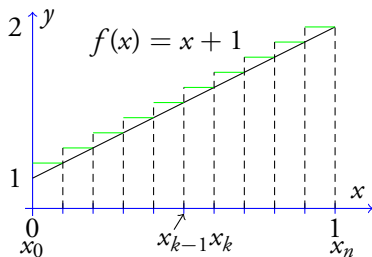
Integral med trappstegfunktioner



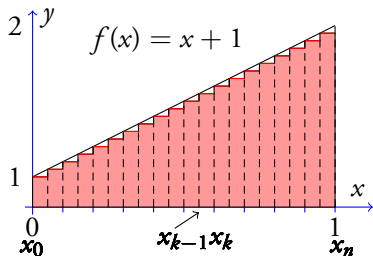
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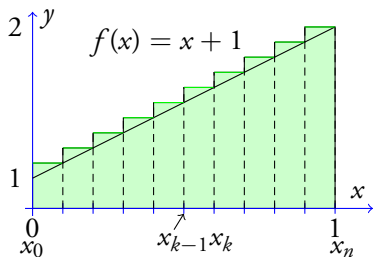
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Integral med trappstegfunktioner



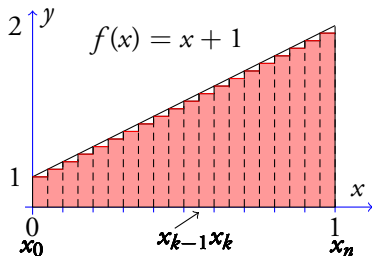
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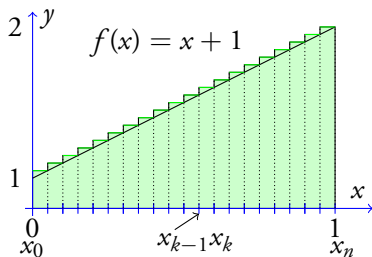
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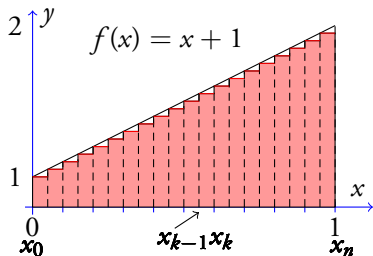
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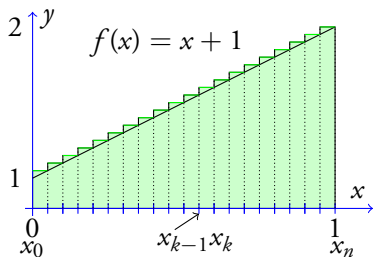
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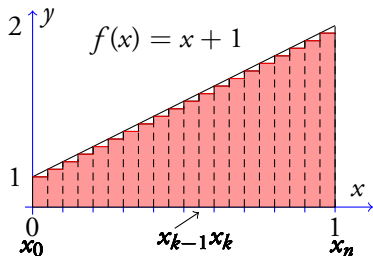
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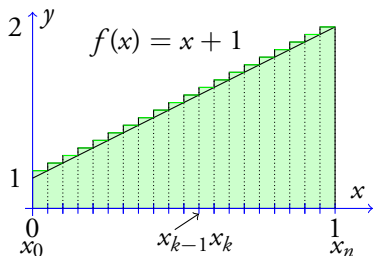
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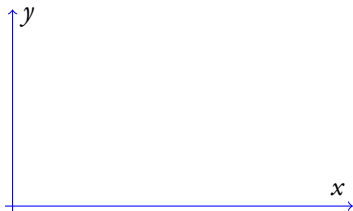
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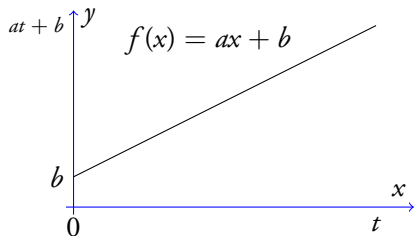
Integral med variabel övergräns



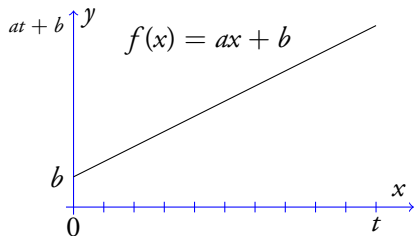
Integral med variabel övergräns



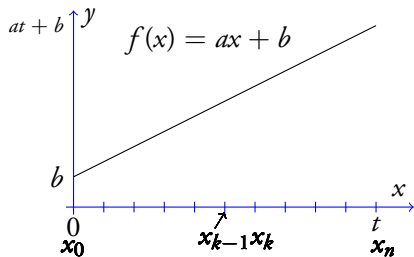
Integral med variabel övergräns



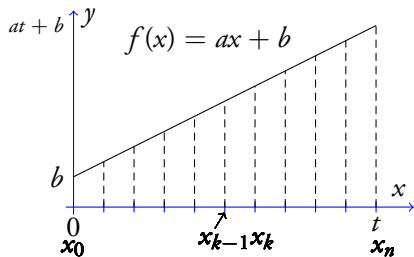
Integral med variabel övergräns



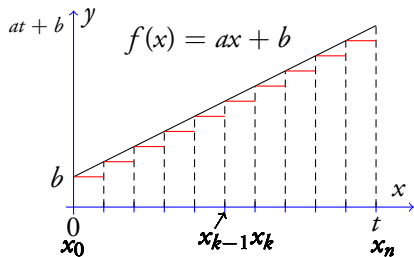
Integral med variabel övergräns



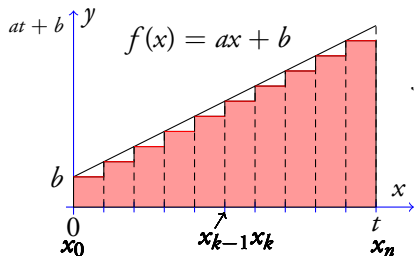
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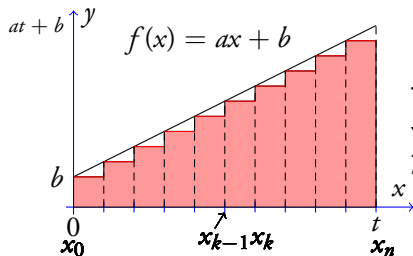
Integral med variabel övergräns



$$\int_0^t \Phi_n(x) dx = \sum_{k=1}^n f(x_{k-1})(x_k - x_{k-1}) =$$



Integral med variabel övergräns

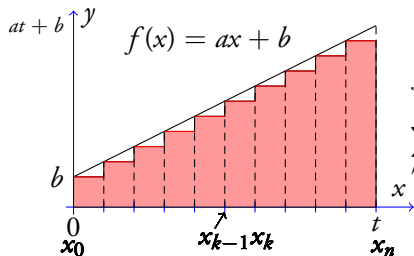


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Integral med variabel övergräns



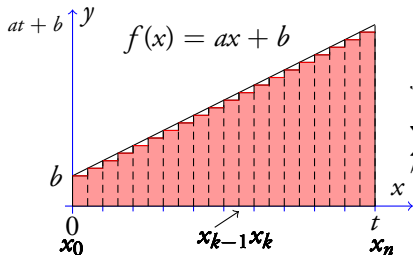
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Integral med variabel övergräns



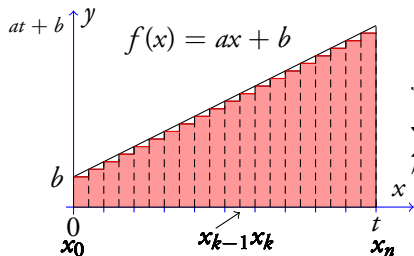
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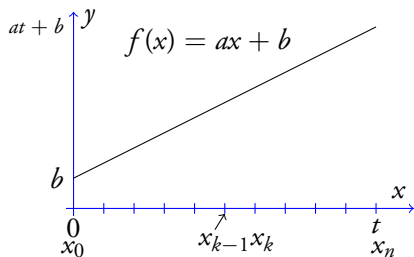
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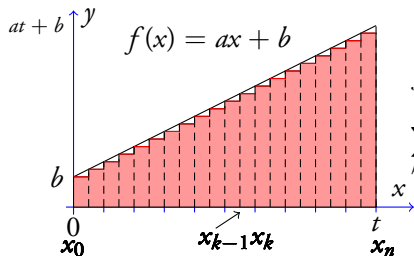
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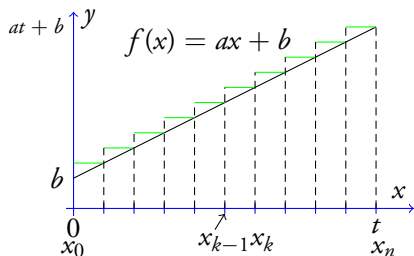
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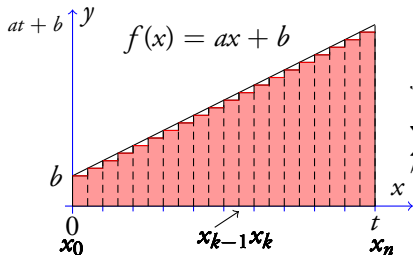
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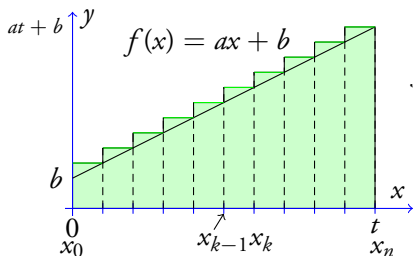
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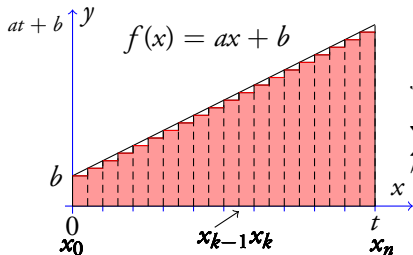
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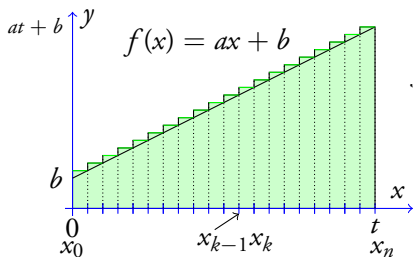
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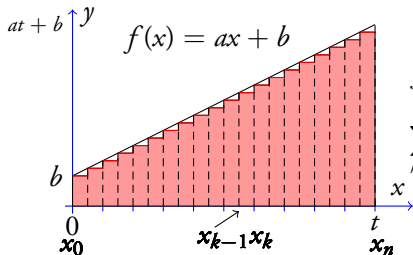
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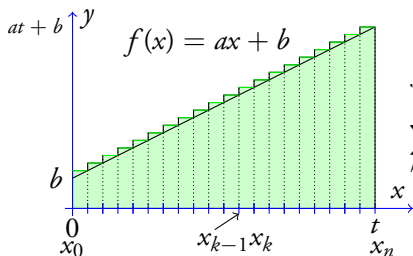
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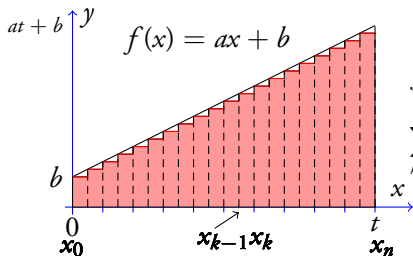
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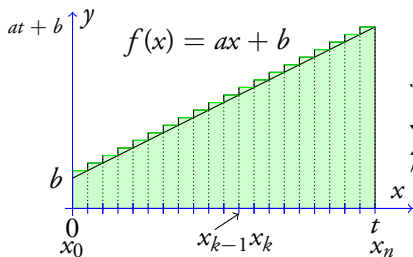
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