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350

Image Analysis (FMAN20) Lecture 1, 2019

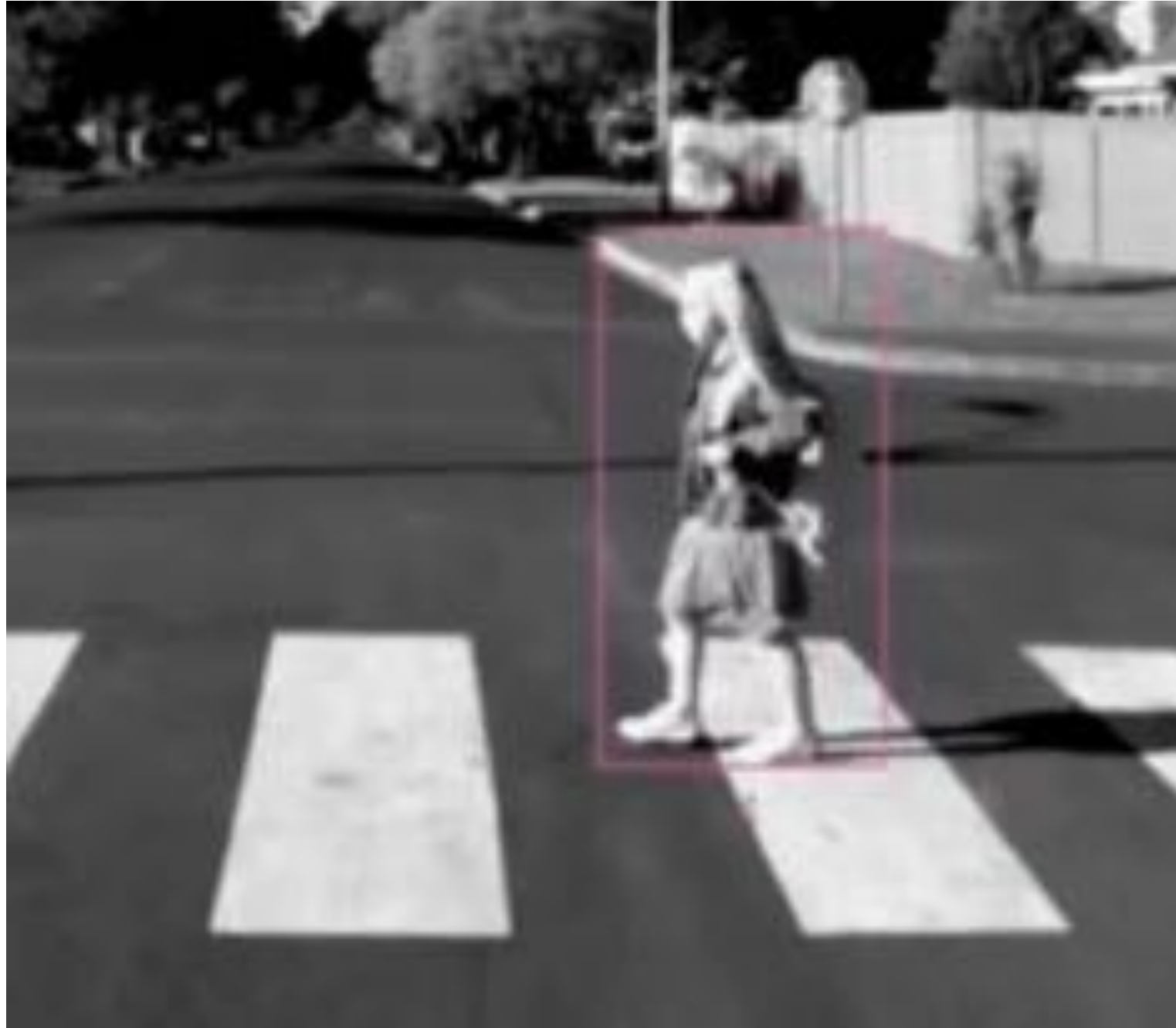
MAGNUS OSKARSSON



Image Analysis - Motivation



Image Analysis - Motivation



Overview

1. Image Analysis – examples
2. Image Models (continuous vs discrete)
3. Sampling and interpolation
4. Discrete geometry

PrimaryText




Computer Vision: Alg...

← → ↻ ↺ ☆ <http://research.microsoft.com/en-us/um/people/szeliski/Book/>

📧 Gmail 📄 Manuscript Central 📄 cvpr.ac 📄 EE364a: Lecture Slides 📄 KeepVid: Download ... 📄 LBA A-Z

Computer Vision: Algorithms and Applications

(c) [Richard Szeliski](#), Microsoft Research



Welcome to the repository for drafts of my computer vision textbook.

This book is largely based on the computer vision courses that I have co-taught at the University of Washington ([2008](#), [2005](#), [2001](#)) and Stanford (2003) with [Steve Seitz](#) and [David Fleet](#).

While I am working on the book, I would *love* to have people "test-drive" it in their computer vision courses (or their research) and [send me feedback](#).

The PDFs should be enabled for commenting directly in your viewer. Also, hyper-links to sections, equations, and references are enabled. To get back to where you were, use Alt-Left-Arrow in Acrobat.

This Web site is also a placeholder for the site that will accompany my computer vision textbook once it is published. Once I get further along with the project, I hope to publish supplemental course material here, such as figures and images from the book, slides sets, pointers to software, and a bibliography.

Latest draft

[June 19, 2009](#) (minor updates)

Mathematical Imaging Group

- Mathematical Imaging Group
 - 3 prof, 4 lecturers, 15-20 phd students
 - Mathematics and mathematical statistics
- Centre for Mathematical Sciences
 - Mathematics (appr. 80 employees)
 - Mathematical statistics (appr. 30 employees)
 - Numerical Analysis (appr. 10 employees)

Research

- Geometry (3D shape, camera calibration, camera motion , structure and motion, robotics)
- Medical Image Analysis (Shape variation, segmentation, tomography, decision support)
- Cognitive Vision (recognition, detection, scene interpretation, attention, segmentation, handwriting recognition)

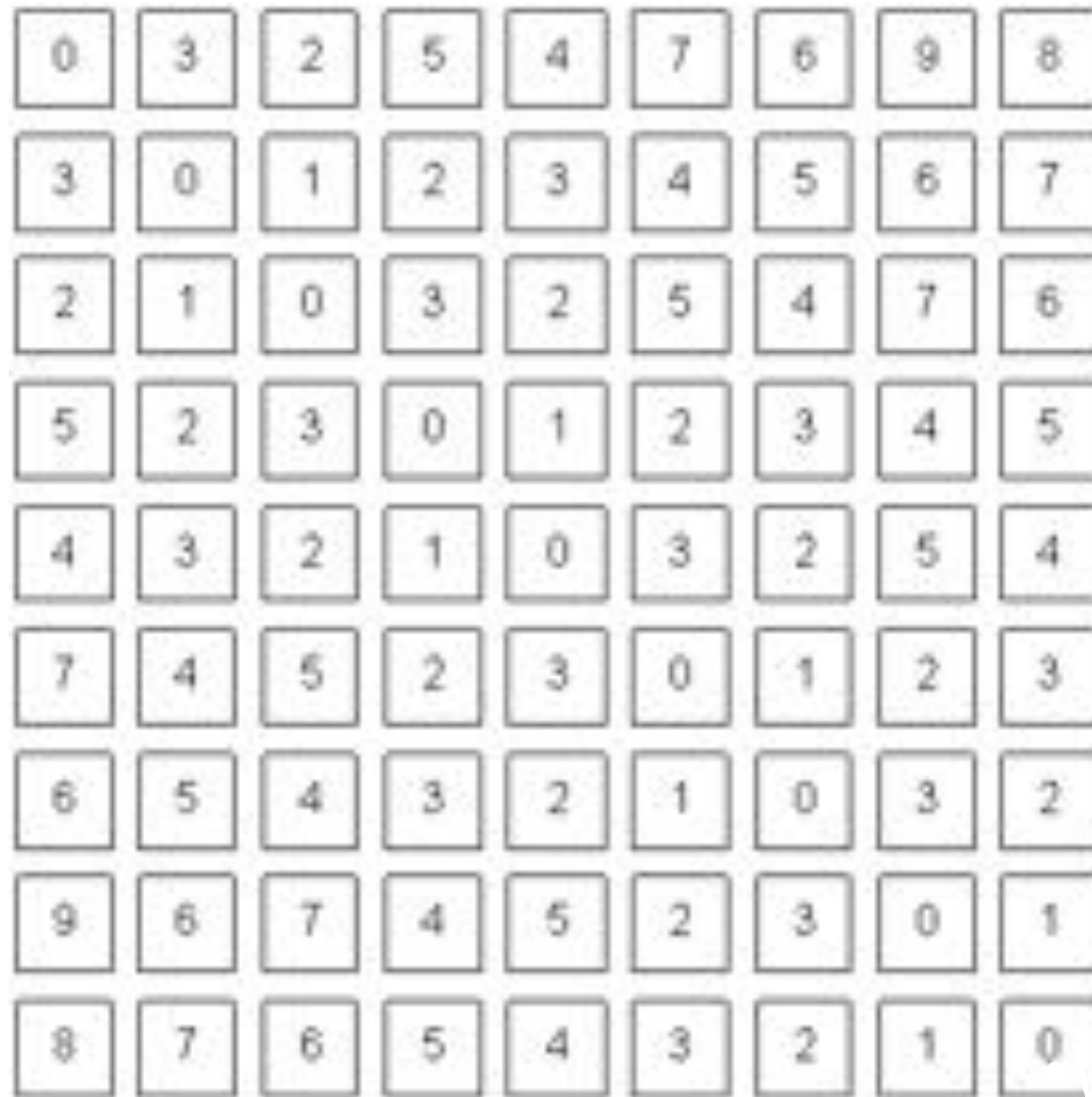
The goal of Image analysis

- To bridge the gap between pixels and “meaning”

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

The goal of Image analysis

- To bridge the gap between pixels and “meaning”

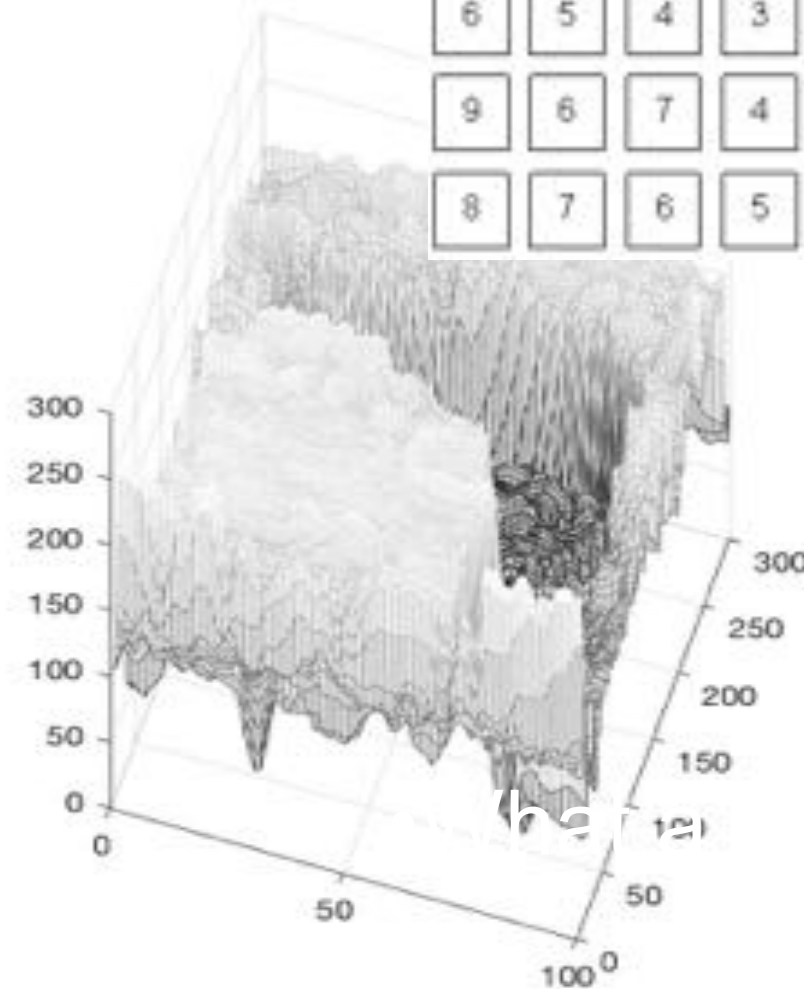
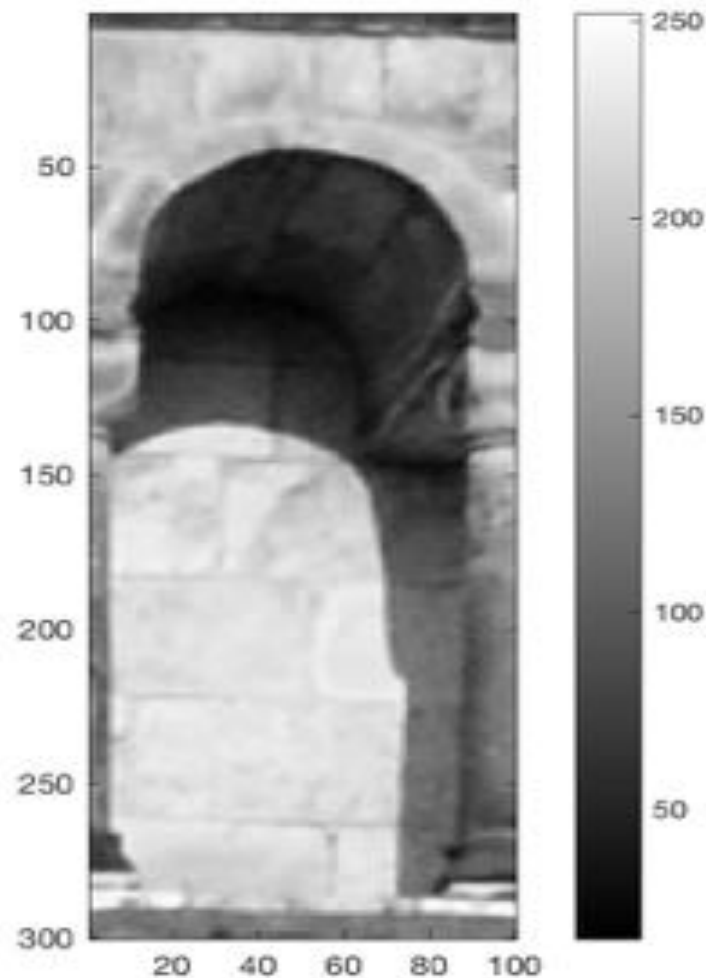


The goal of Image analysis

- Images are functions. Each pixel measures brightness

$$f : \mathbf{Z}^2 \rightarrow \mathbf{Z}$$

- What we see



0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

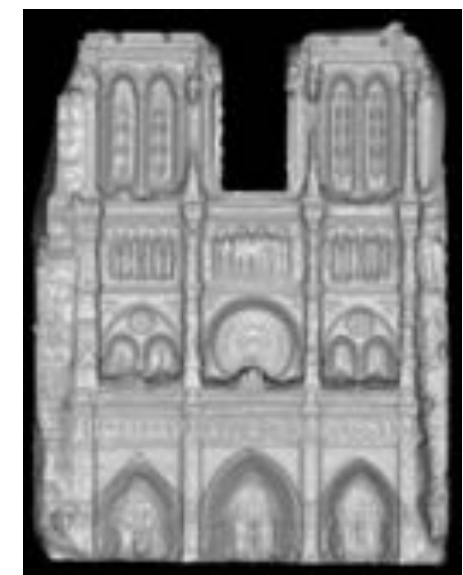
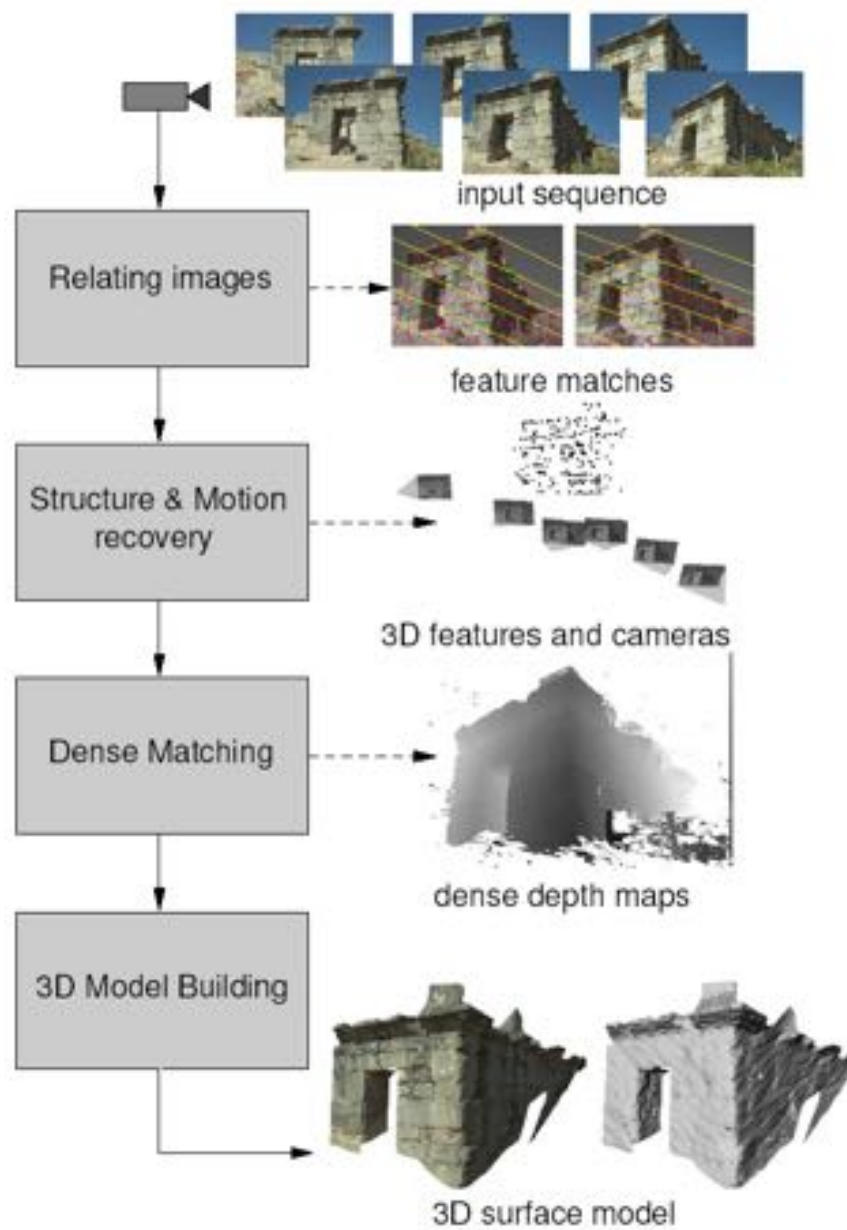
Why images?

- As image sources multiply, so do applications
 - Relieve humans of boring, easy tasks
 - Enhance human abilities: human-computer interaction, visualization
 - Perception for robotics / autonomous agents
 - Organize and give access to visual content

What kind of information can we extract from an image?

- Metric 3D information
- Semantic information
- Think about tasks that you solve with your own eyes!

Vision as measurement device



- Vision as a source of semantic information



•Object categorization



•sky

•building

•flag

•banner

•face

•wall

•street lamp

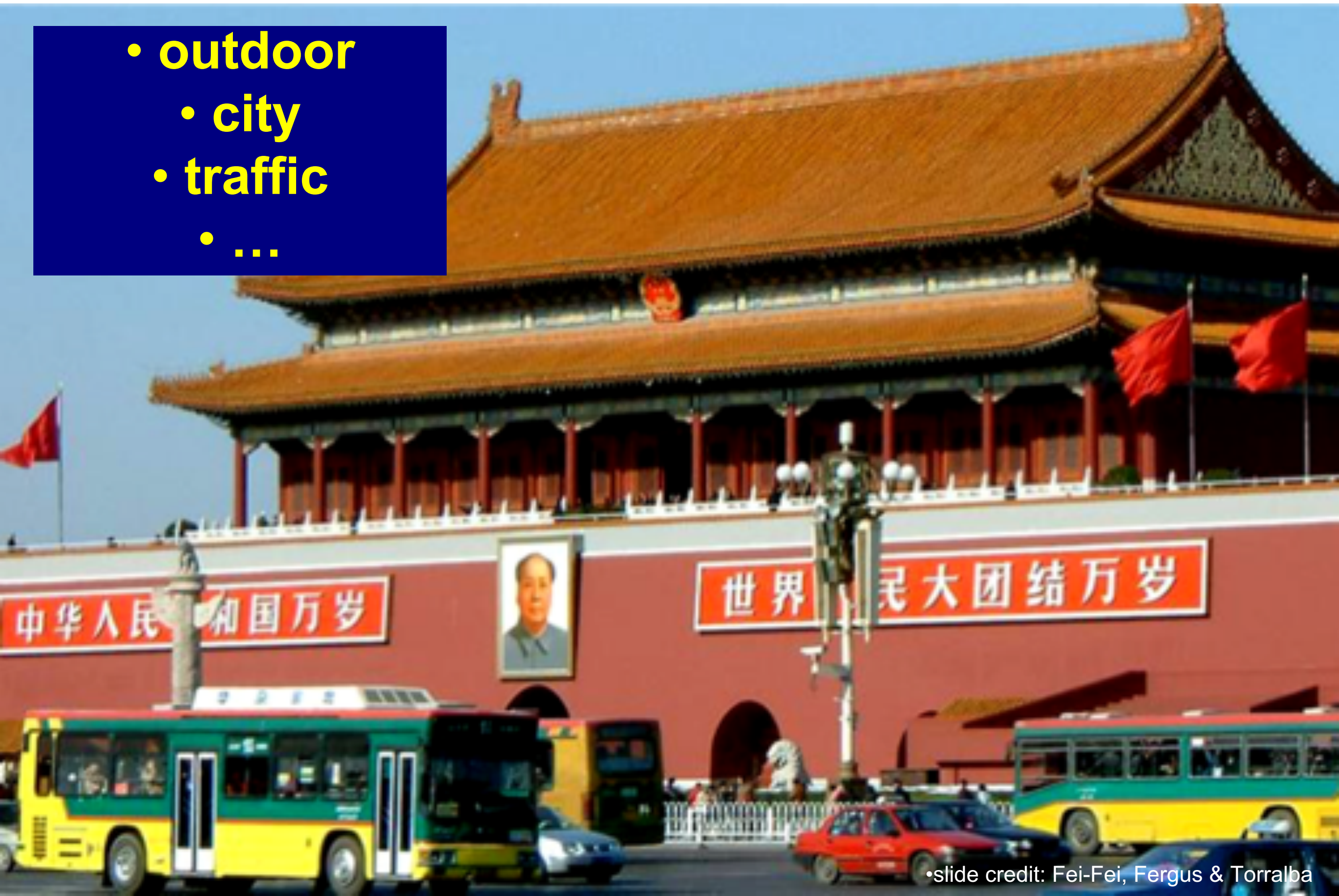
•bus

•bus

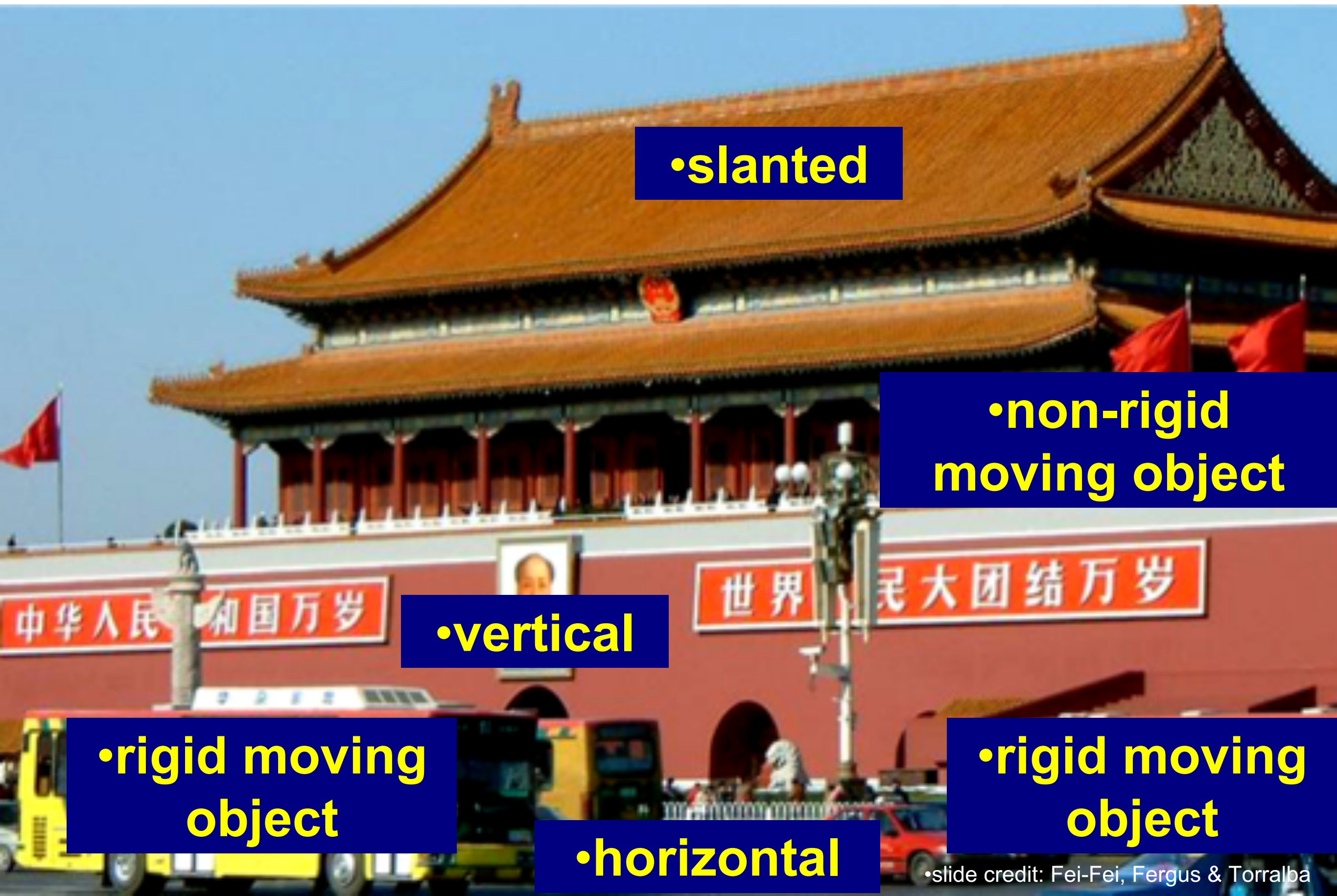
•cars

• Scene and context categorization

- outdoor
 - city
 - traffic
 - ...



- Qualitative spatial information



•slanted

•non-rigid
moving object

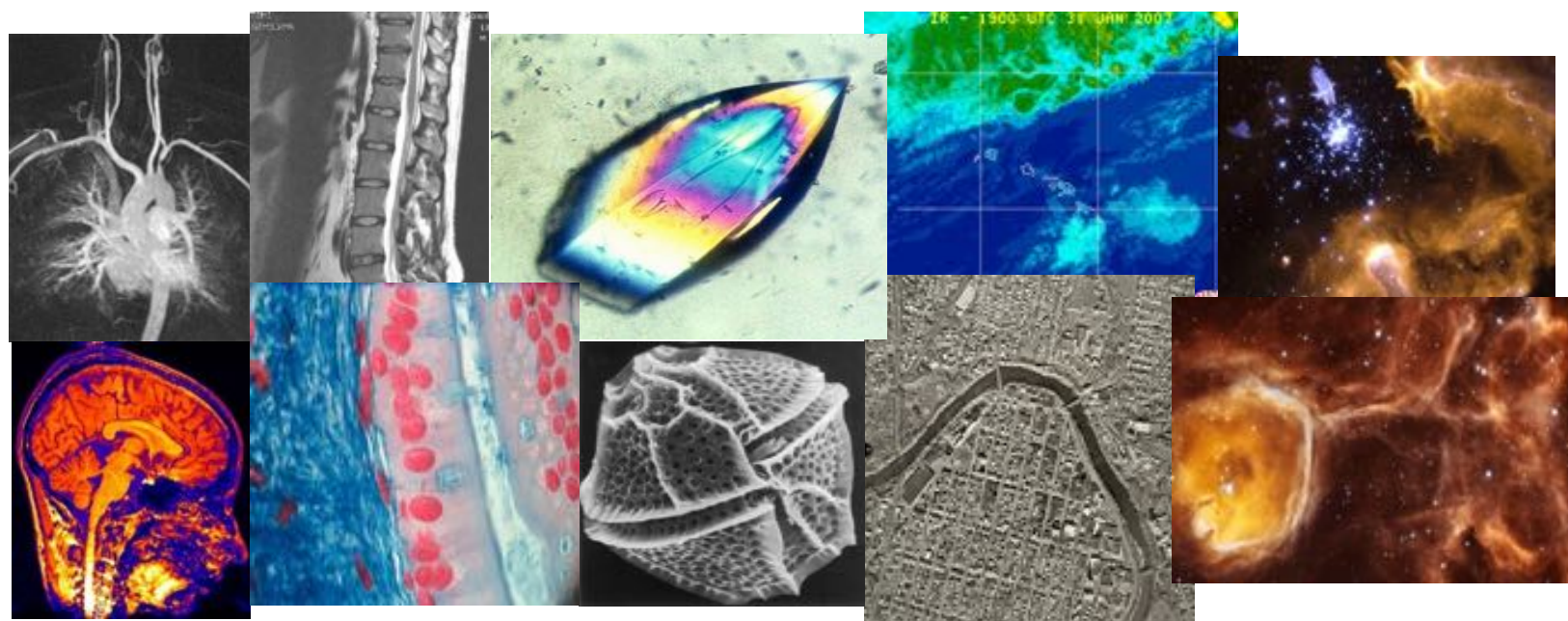
•vertical

•rigid moving
object

•horizontal

•rigid moving
object

- Vision is useful: Images and video are everywhere!



Why is working with images
challenging/difficult?

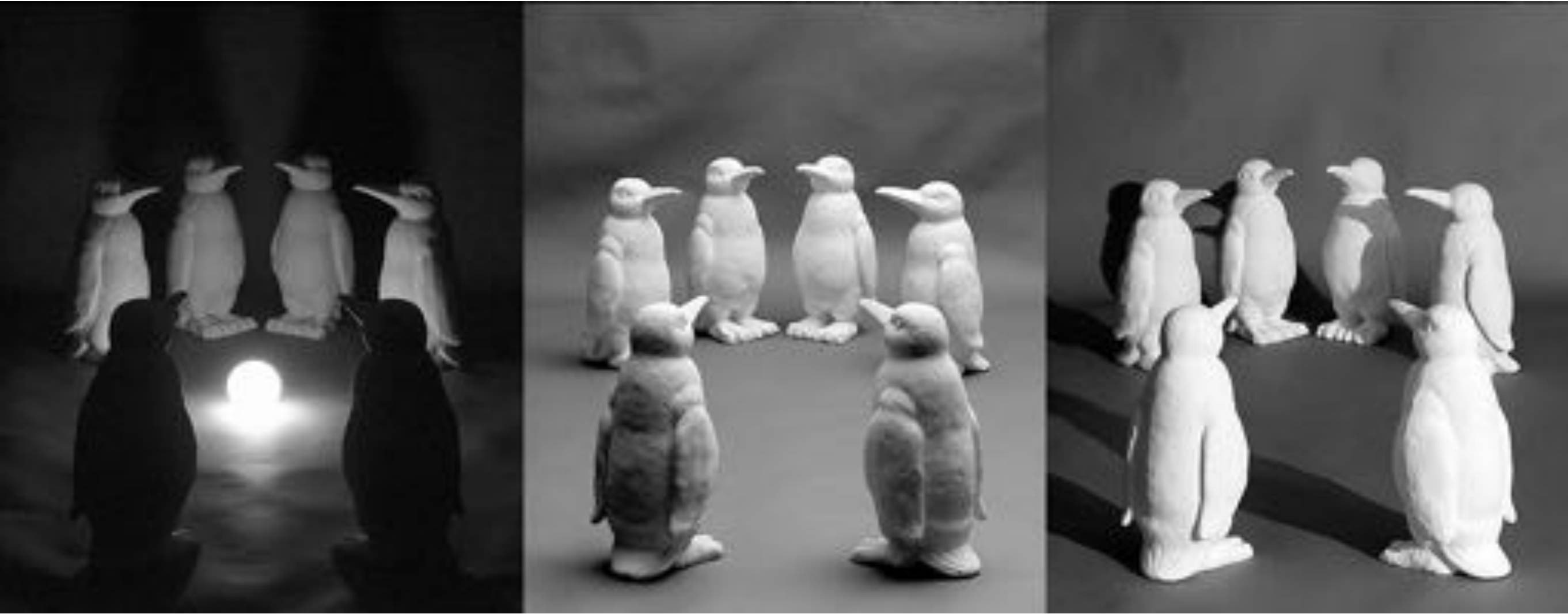
- Challenges: viewpoint variation



- Michelangelo 1475-1564

- slide credit: Fei-Fei, Fergus & Torralba

- Challenges: illumination



- Challenges: scale



•slide credit: Fei-Fei, Fergus & Torralba

- Challenges: deformation



- Xu, Beihong 1943

- Challenges: occlusion



- Magritte, 1957

•slide credit: Fei-Fei, Fergus & Torralba

- Challenges: background clutter



Emperor shrimp and commensal crab on a sea cucumber in the Philippines.
Photograph by Tim Laman

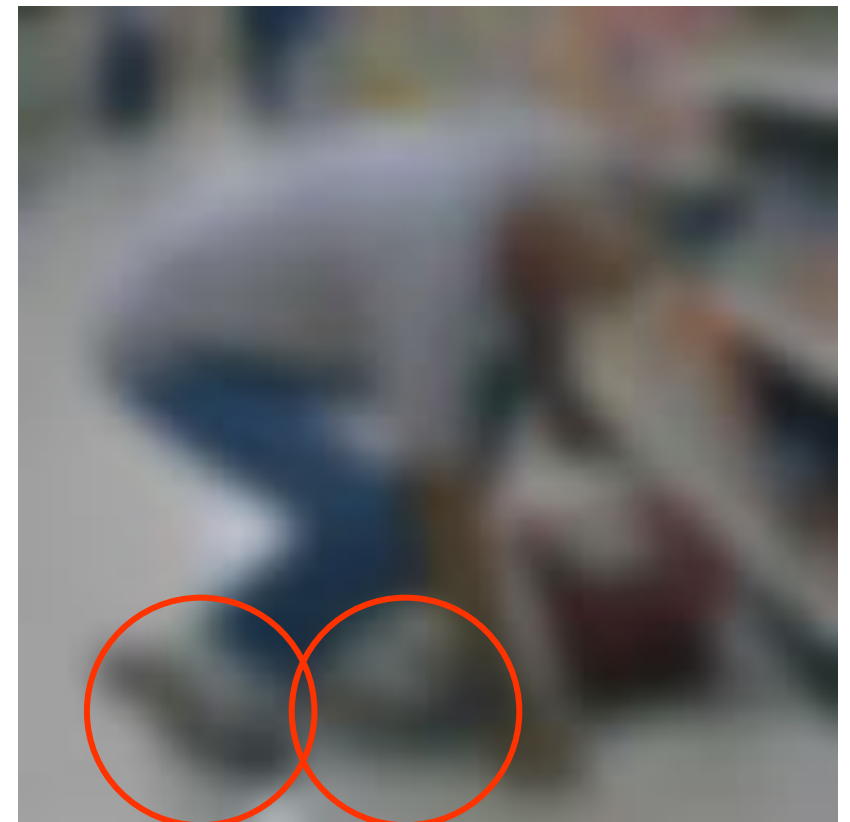
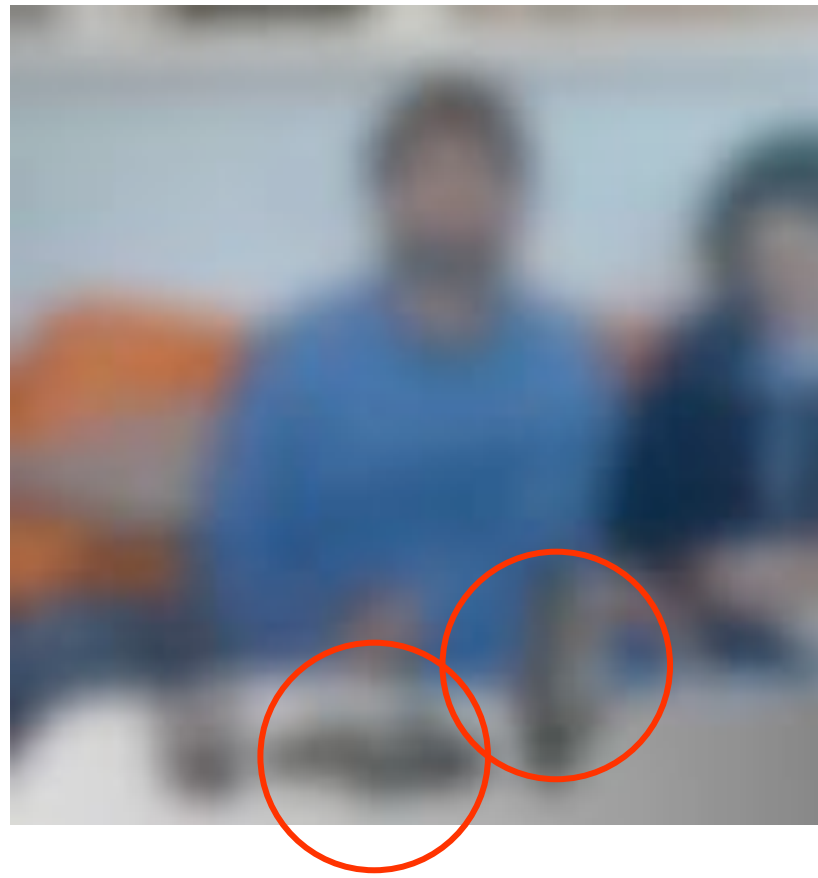
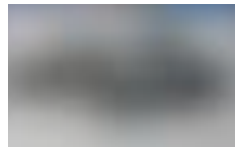
•Challenges: Motion



Challenges: object intra-class variation



Challenges: local ambiguity



Challenges: context



Challenges: context



Challenges: context



In this course

- Tools:
 - Basics of image modelling
 - Linear Algebra, Linear System Theory
 - Filters
 - Mathematical Statistics
 - Machine Learning
 - Segmentation
- System development
 - Based on the tools
 - Ground truth, evaluation, benchmarking

After the course

- You should be able to develop and test your own image analysis system
- You should have tools for understanding and working with big data
- You should have improved your skills in programming and modelling.

Continuous Model

An image can be seen as a function

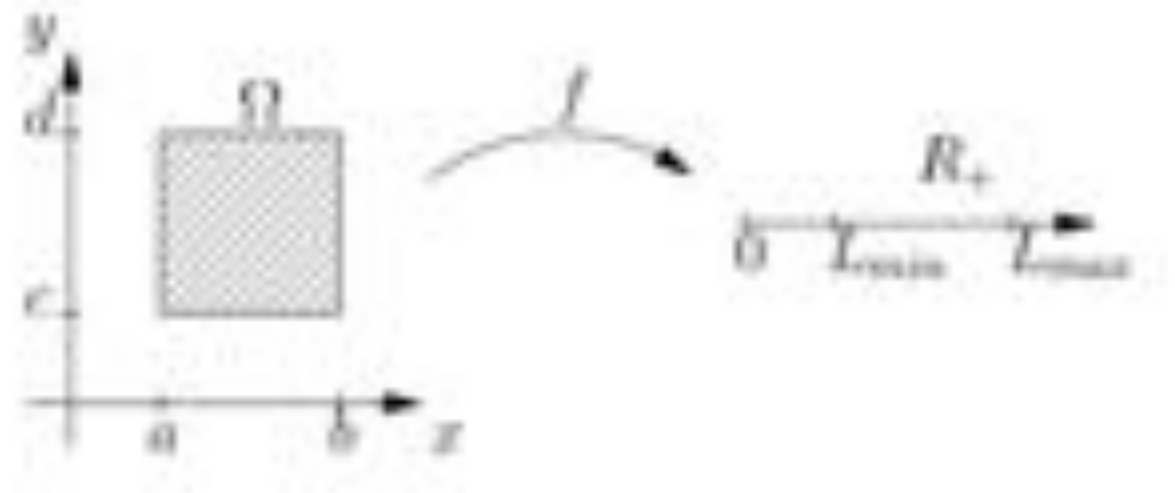
$$f : \Omega \mapsto \mathbb{R}_+ ,$$

where $\Omega = \{ (x, y) \mid a \leq x \leq b, c \leq y \leq d \} \subseteq \mathbb{R}^2$ and $\mathbb{R}_+ = \{x \in \mathbb{R} \mid x \geq 0\}$. $f(x, y)$ = intensity at point (x, y) = gray-level

(f does not have to be continuous)

$$0 \leq L_{min} \leq f \leq L_{max} \leq \infty$$

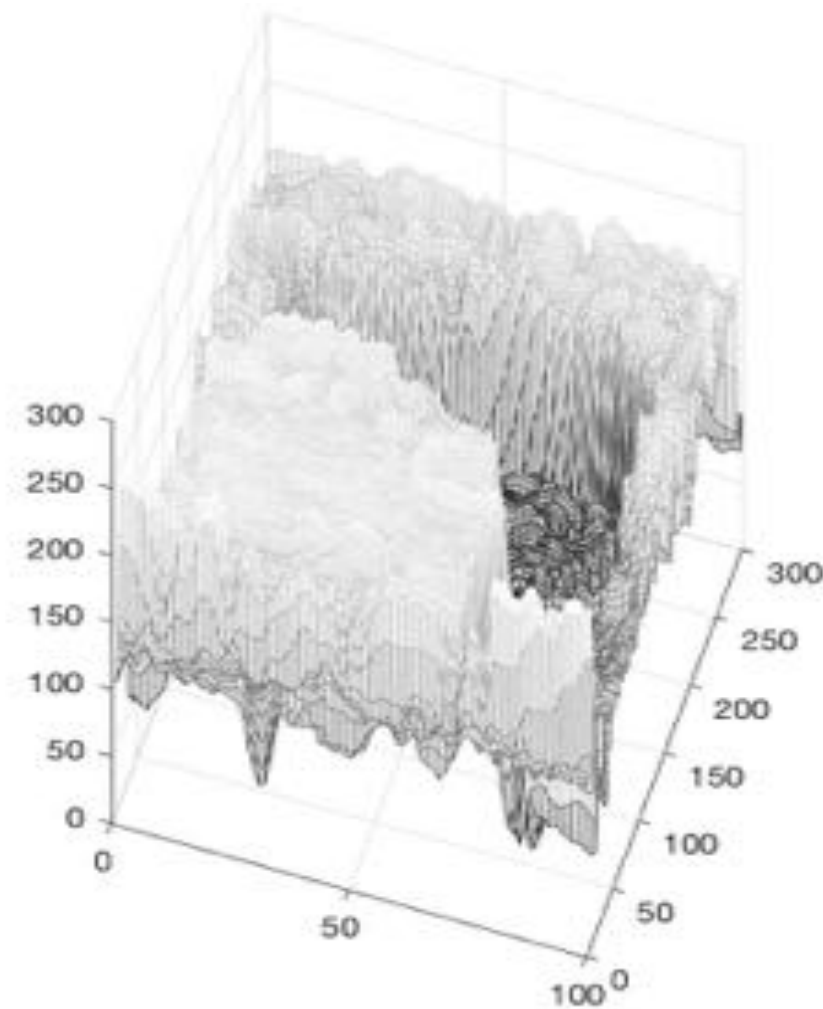
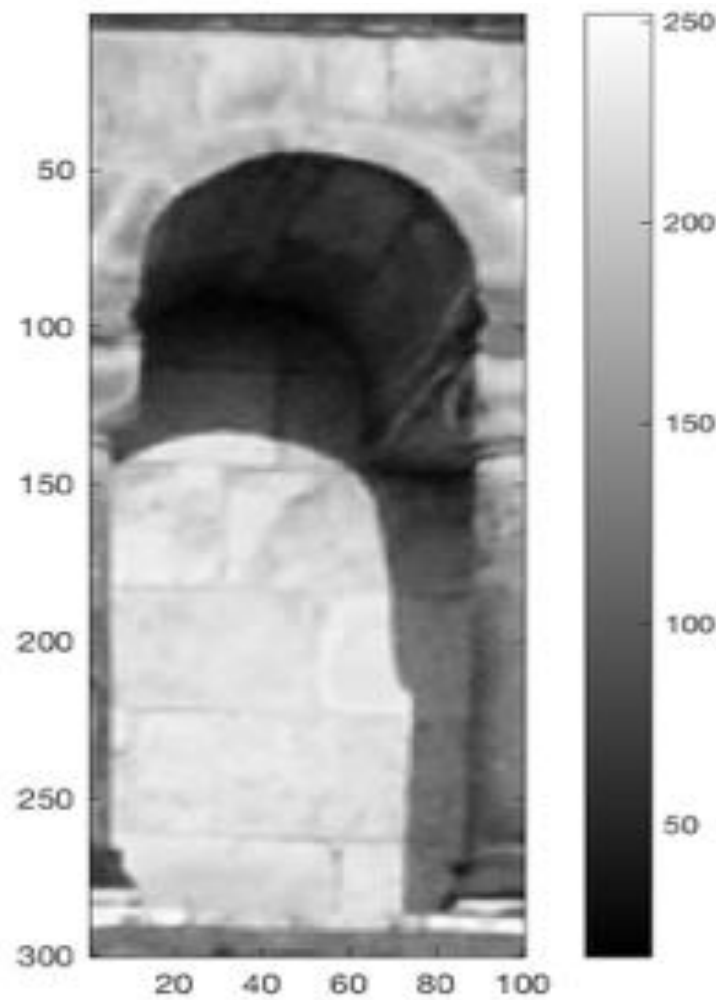
$[L_{min}, L_{max}]$ = gray-scale



Continuous Model

An image can be seen as a function

$$f : \Omega \mapsto \mathbb{R}_+$$

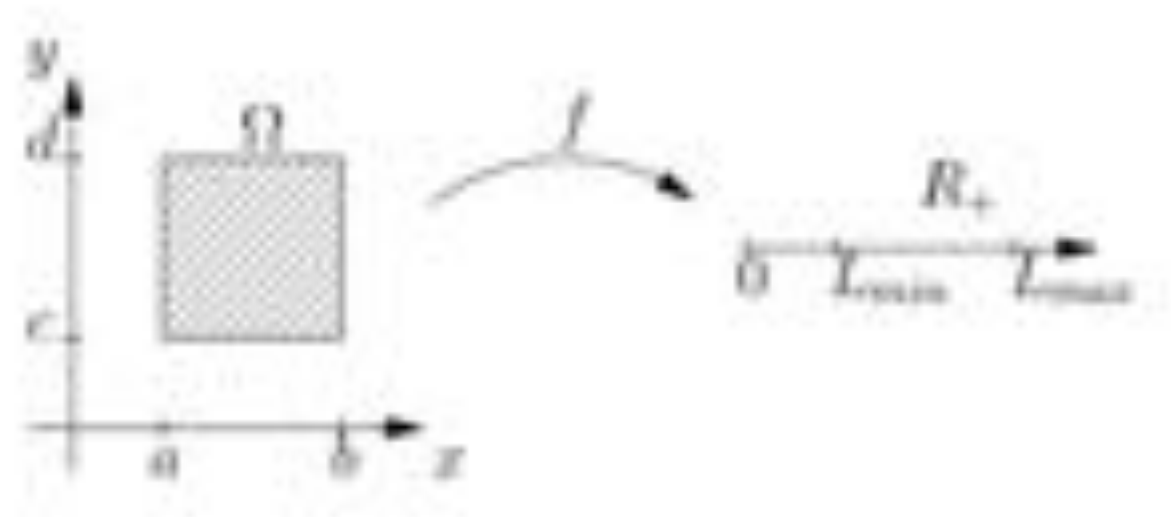


Discrete Image Model

- Discretize $x, y \rightarrow$ sampling M rows, N columns
- Discretize $f \rightarrow$ quantization
 - (often in 2^m levels)
 - Color depth
 - "8 bit grayscale", $2^8 = 256$ levels, 0-255

$$f : \Omega \mapsto \mathbf{Z} \quad \Omega \subset \mathbf{Z}^2$$

- Decreasing M and N
 - Chess patterns
- Decreasing m
 - False contours



Sampling, decreasing M and N



Sampling, decreasing M and N



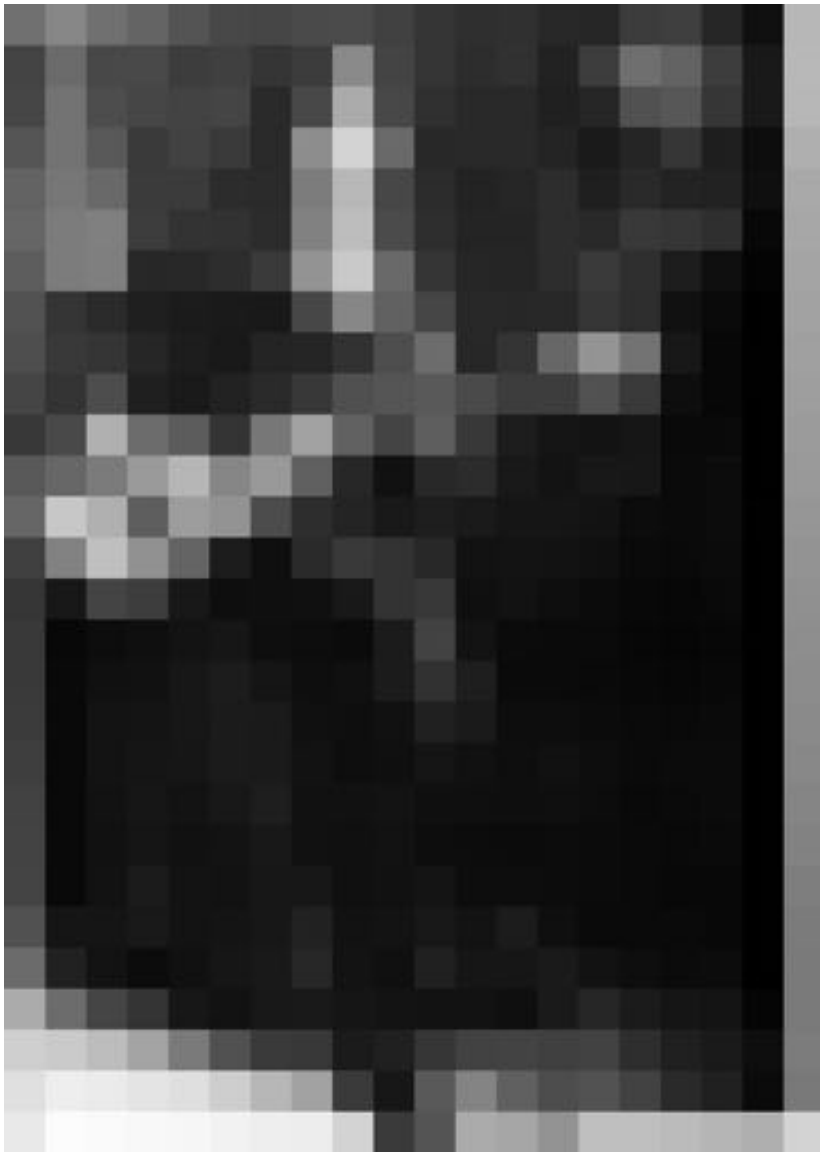
Sampling, decreasing M and N



Sampling, decreasing M and N



Sampling, decreasing M and N



Sampling, decreasing M and N



Quantization, decreasing m



Quantization, decreasing m



Quantization, decreasing m



Quantization, decreasing m



Interpolation

- Discrete image $f : \mathbb{Z}^2 \rightarrow \mathbb{R}$
- Continuous image $F : \mathbb{R}^2 \rightarrow \mathbb{R}$
- Going from F to f (sampling)

$$f(i, j) = D(F)(i, j) = F(i, j)$$

- Going from f to F (interpolation)

$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$

Interpolation

- Discrete image $f : \mathbb{Z}^2 \rightarrow \mathbb{R}$
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Interpretation:

Place a hump h at each pixel

Scale the hump by $f(i, j)$

Add together

Interpolation

- Discrete image $f : \mathbb{Z}^2 \rightarrow \mathbb{R}$
- Continuous image $F : \mathbb{R}^2 \rightarrow \mathbb{R}$
- Going from F to f (sampling)

$$f(i, j) = D(F)(i, j) = F(i, j)$$

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$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$



Different choices of h (different humps)

-> different types of interpolation

Interpolation – what is h?

- How can you find h from method?

$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$

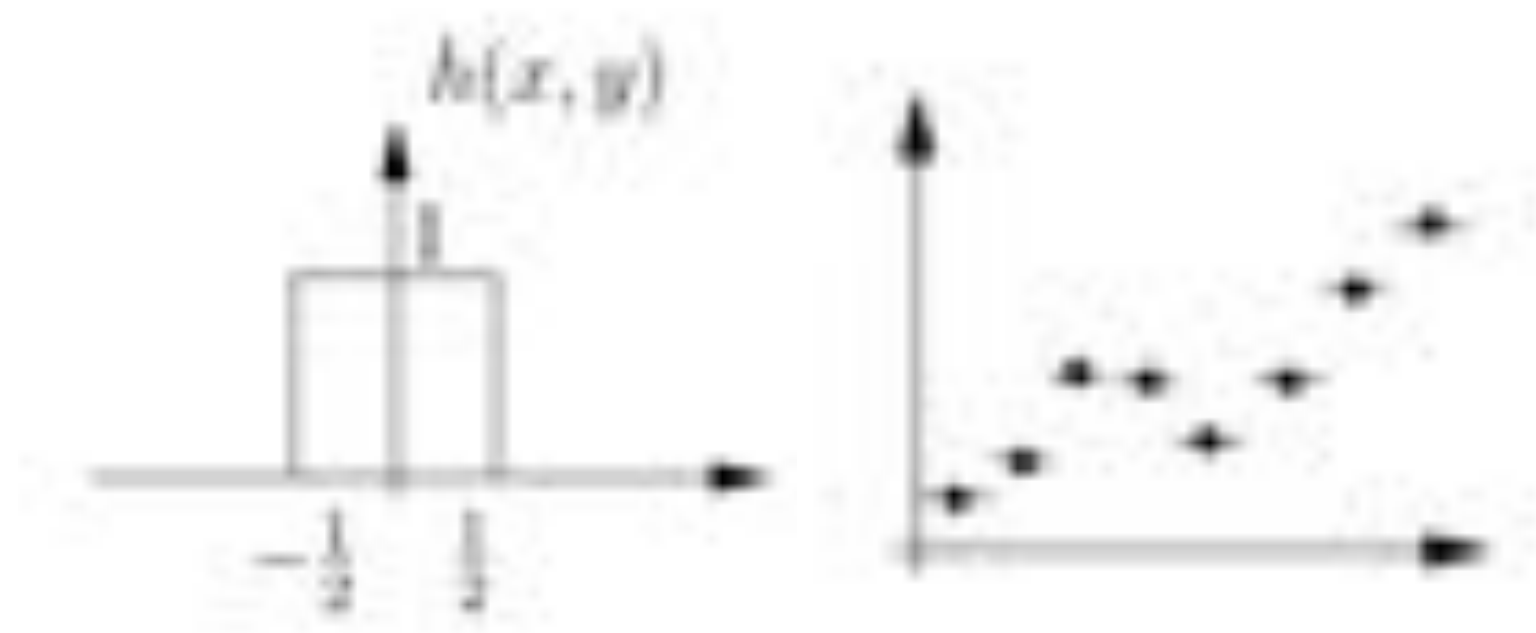
Interpolation

$$f : \mathbb{Z}^2 \rightarrow \mathbb{R}$$
$$F : \mathbb{R}^2 \rightarrow \mathbb{R}$$

- Going from f to F (interpolation)

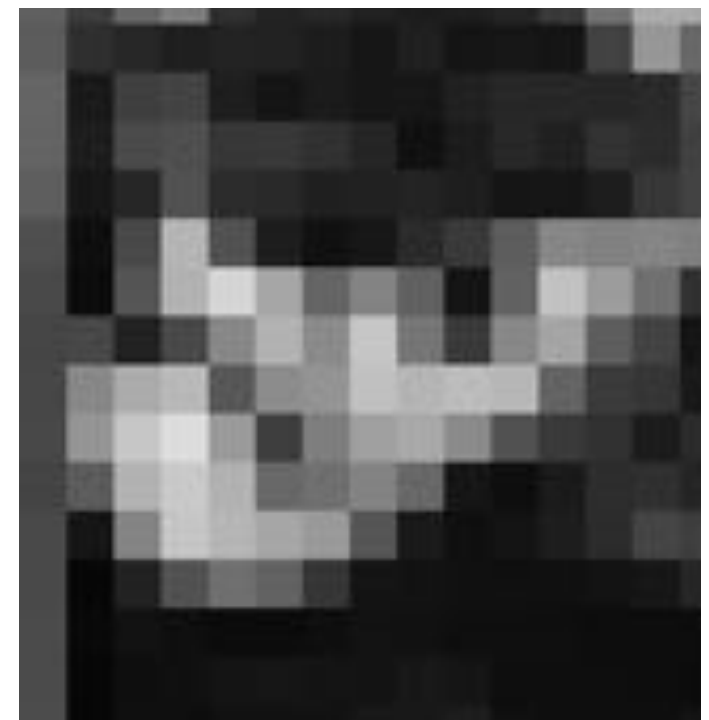
$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$

- Example 1 – Pixel Replication



In 1D

In 2D



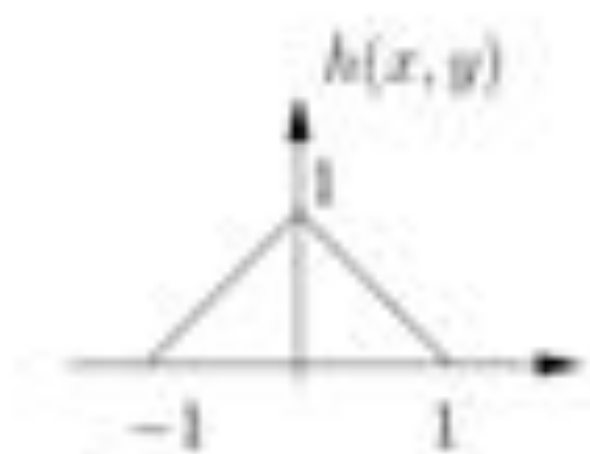
Interpolation

$$f : \mathbb{Z}^2 \rightarrow \mathbb{R}$$
$$F : \mathbb{R}^2 \rightarrow \mathbb{R}$$

- Going from f to F (interpolation)

$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$

- Example 2 – Linear interpolation
- (In two dimensions the corresponding function is bilinear)



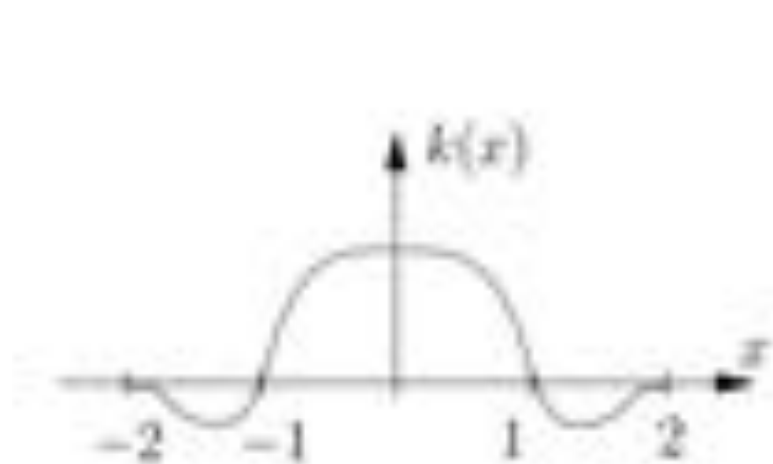
Interpolation

$$f : \mathbb{Z}^2 \rightarrow \mathbb{R}$$
$$F : \mathbb{R}^2 \rightarrow \mathbb{R}$$

- Going from f to F (interpolation)

$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$

- Example 3 – Cubic interpolation
- (In two dimensions the corresponding function is bicubic)



Interpolation

$$f : \mathbb{Z}^2 \rightarrow \mathbb{R}$$
$$F : \mathbb{R}^2 \rightarrow \mathbb{R}$$

- Going from f to F (interpolation)

$$F_h(x, y) = I_h(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} h(x - i, y - j) f(i, j)$$

- Example 4 – Ideal Interpolation

$$\text{sinc}(x) = \begin{cases} \frac{\sin \pi x}{\pi x}, & x \neq 0 \\ 1, & x = 0 \end{cases}$$

$$F(x, y) = I(f)(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} \text{sinc}(x - i) \text{sinc}(y - j) f(i, j).$$

Interpolation

- Discrete image $f : \mathbb{Z}^2 \rightarrow \mathbb{R}$
- Continuous image $F : \mathbb{R}^2 \rightarrow \mathbb{R}$
- If the function F is square integrable, i.e.

$$\int_{x=-\infty}^{\infty} \int_{y=-\infty}^{\infty} |F(x, y)|^2 dx dy$$

- Is bounded.
- If also the fourier transform is zero outside $[-\pi, \pi] \times [-\pi, \pi]$.
- Then

$$I(D(F)) = F.$$

Digital Geometry

Let \mathbb{Z} be the set of integers $0, \pm 1, \pm 2, \dots$.

Grid: \mathbb{Z}^2 ,
 $\begin{matrix} & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ & \cdot & \cdot & \cdot & \cdot \end{matrix}$

Grid point: (x, y)

Definition

4-neighbourhood to (x, y) :

$$N_4(x, y) = \begin{pmatrix} \cdot & \times & \cdot \\ \times & (x, y) & \times \\ \cdot & \times & \cdot \end{pmatrix} .$$



Digital Geometry

Definition

p and q are **4-neighbours** if $p \in N_4(q)$. ■

Definition

A **4-path** from p to q is a sequence

$$p = r_0, r_1, r_2, \dots, r_n = q ,$$

such that r_i and r_{i+1} are 4-neighbours. ■

Definition

Let $S \subseteq \mathbb{Z}^2$. S is **4-connected** if for every $p, q \in S$ there is a 4-path in S from p to q . ■

There are efficient algorithms for dividing sets $M \subseteq \mathbb{Z}^2$ in connected components. (For example, see MATLAB's `bwlabel`).

Digital Geometry

Similar definitions with other neighbourhood structures

Definition

D -neighbourhood to (x, y) :

$$N_D(x, y) = \begin{pmatrix} \times & \cdot & \times \\ \cdot & (x, y) & \cdot \\ \times & \cdot & \times \end{pmatrix} .$$



Definition

8-neighbourhood to (x, y) :

$$N_8(x, y) = N_4(x, y) \cup N_D(x, y) = \begin{pmatrix} \times & \times & \times \\ \times & (x, y) & \times \\ \times & \times & \times \end{pmatrix} .$$



Digital Geometry (bwlabel)

```
>> bild = [1 1 0 0 0;1 0 0 0 1;0 0 0 0 1;1 1 0 1 1]
```

```
bild =
```

1	1	0	0	0
1	0	0	0	1
0	0	0	0	1
1	1	0	1	1

```
>> segmentering = bwlabel(bild)
```

```
segmentering =
```

1	1	0	0	0
1	0	0	0	3
0	0	0	0	3
2	2	0	3	3

Gray level transformations

Pixelwise operations

A simple method for image enhancement

Definition

Let $f(x, y)$ be the intensity function of an image. A **gray-level transformation**, T , is a function (of one variable)

$$g(x, y) = T(f(x, y))$$
$$s = T(r) ,$$

that changes from gray-level f to gray-level g . T usually fulfils

- ▶ $T(r)$ increasing in $L_{min} \leq r \leq L_{max}$,
- ▶ $0 \leq T(r) \leq L$.

In many examples we assume that $L_{min} = 0$ och $L_{max} = L = 1$. The requirements on T being increasing can be relaxed, e.g. with inversion.

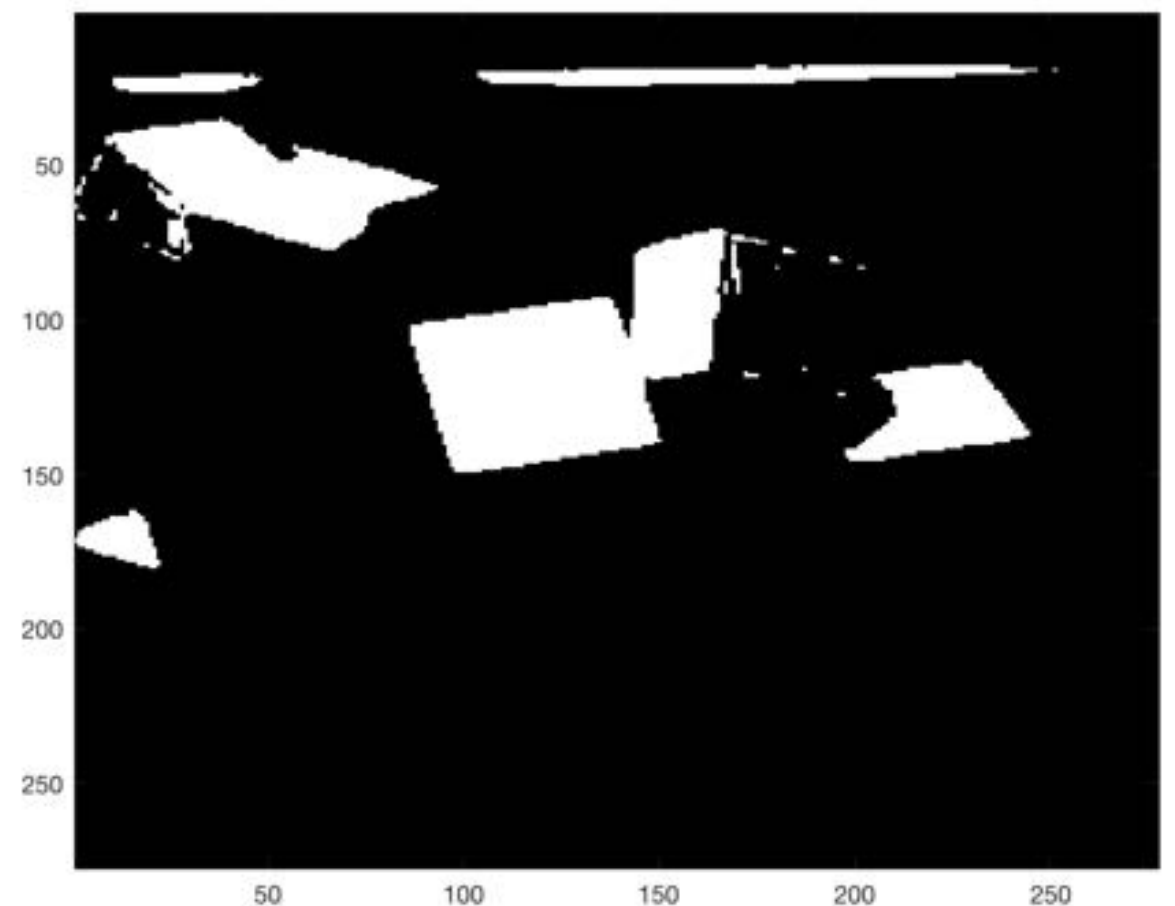
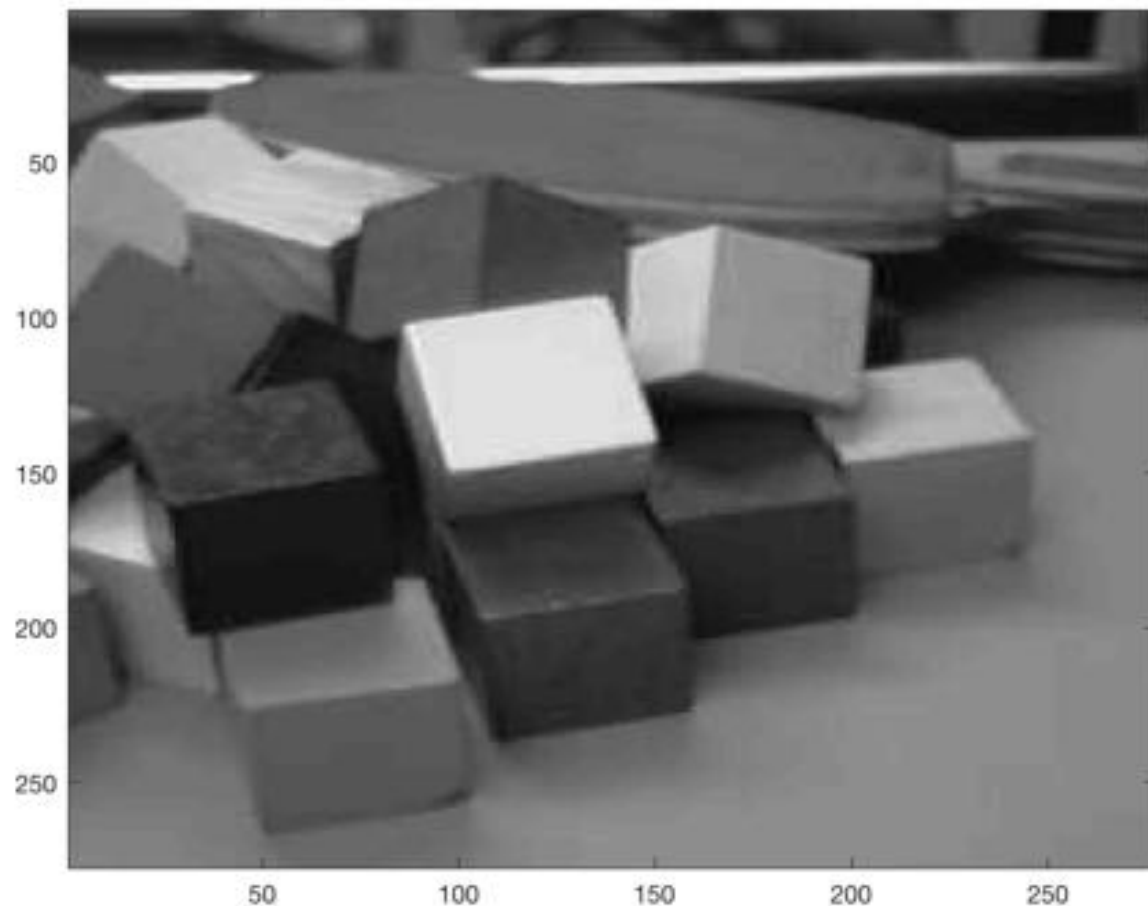
Gray level transformations

Pixelwise operations

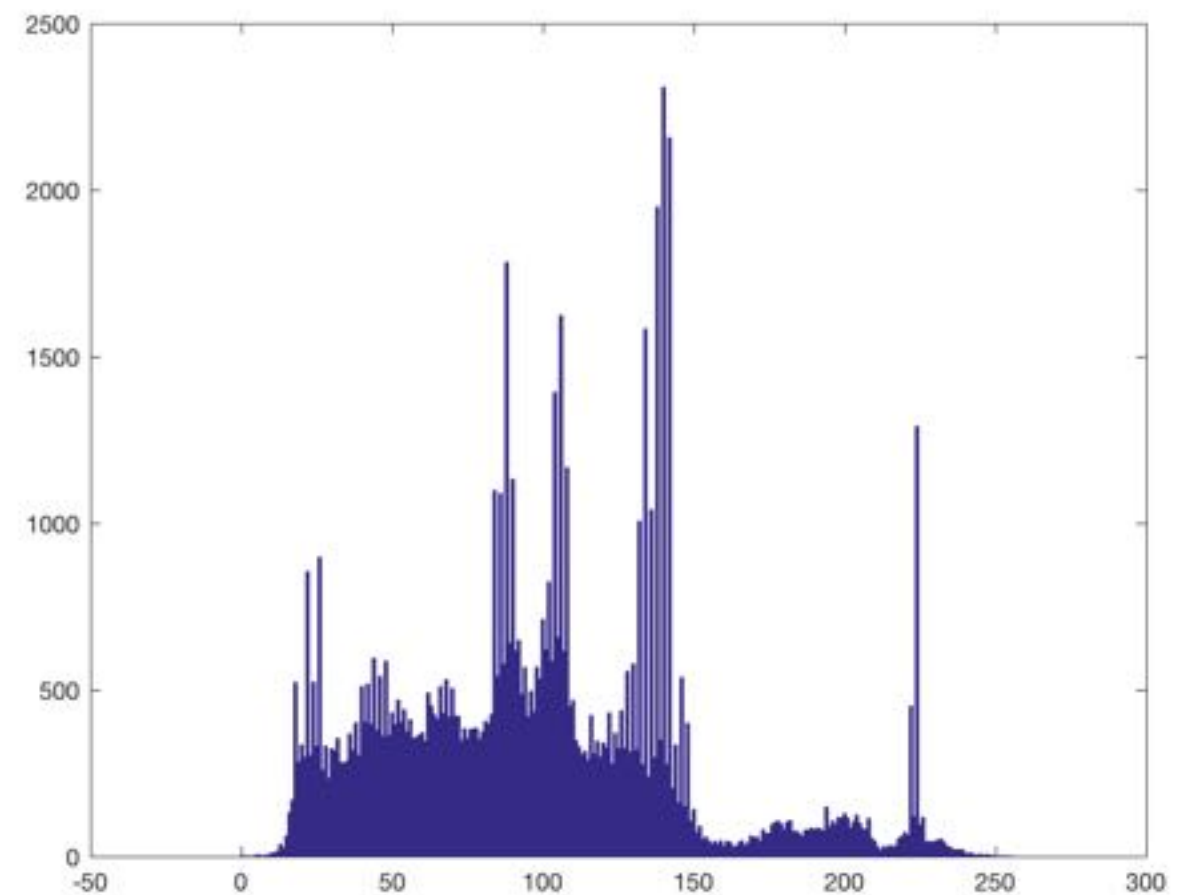
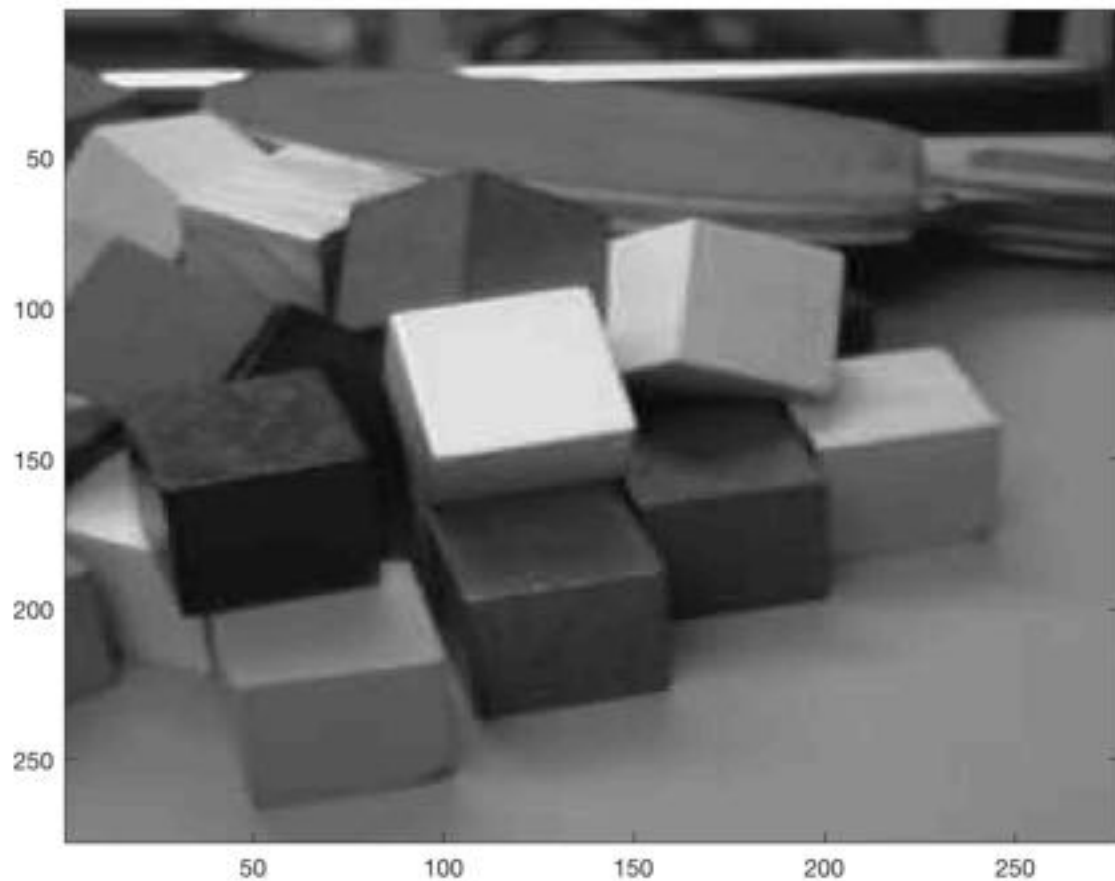
Let

$$T(r) = \begin{cases} 0 & r \leq m \\ 1 & r > m, \end{cases}$$

for some $0 < m < 1$.



Histograms



Histograms

- Let $s = T(r)$ be a gray level transformation
- Let p_r be the histogram before the transformation
- Let p_s be the histogram after the transformation
- Assume that T is a monotonically increasing function.
- The pixels that were darker than level r before are darker than s after.

It follows that

$$\int_0^s p_s(t) dt = \int_0^r p_r(t) dt.$$

Histograms

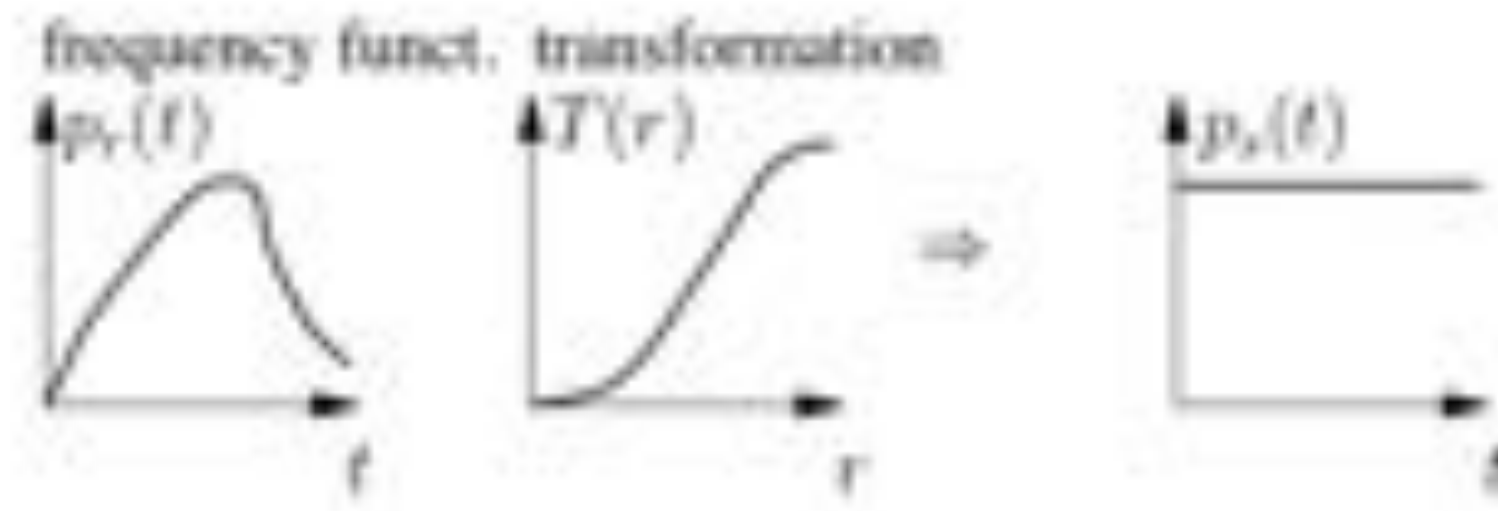
$$\int_0^s p_s(t) dt = \int_0^r p_r(t) dt.$$

Take T so that $p_s(s) = 1$ (constant).

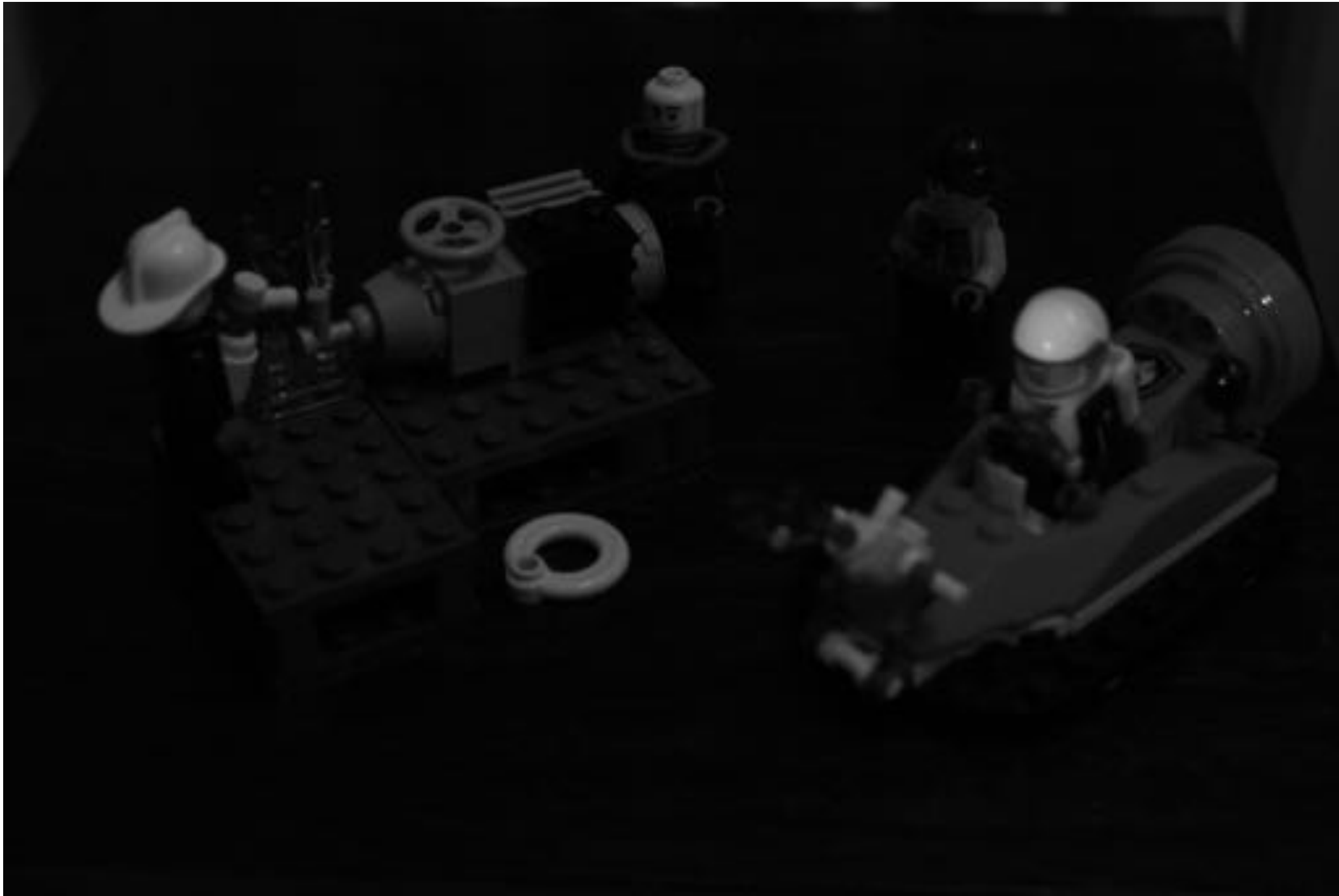
$$\int_0^r p_r(t) dt = \int_0^s 1 dt = s \Rightarrow s = T(r) = \int_0^r p_r(t) dt$$

or

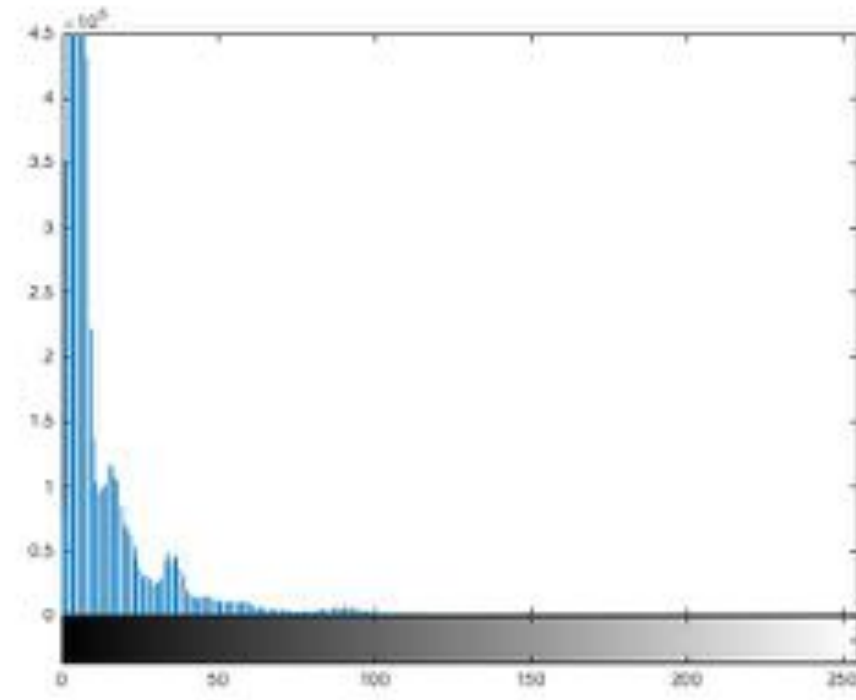
$$\frac{ds}{dr} = p_r(r)$$



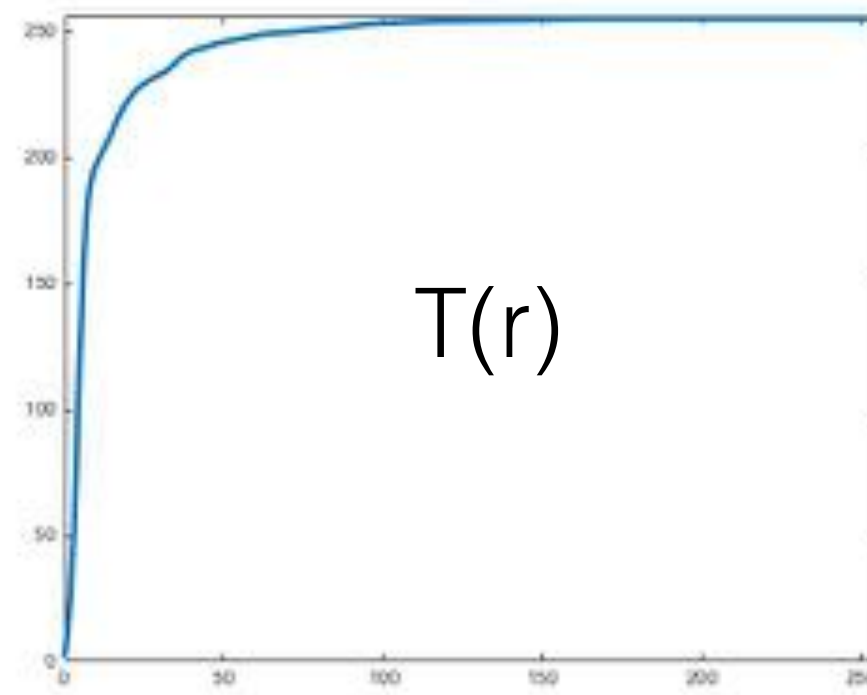
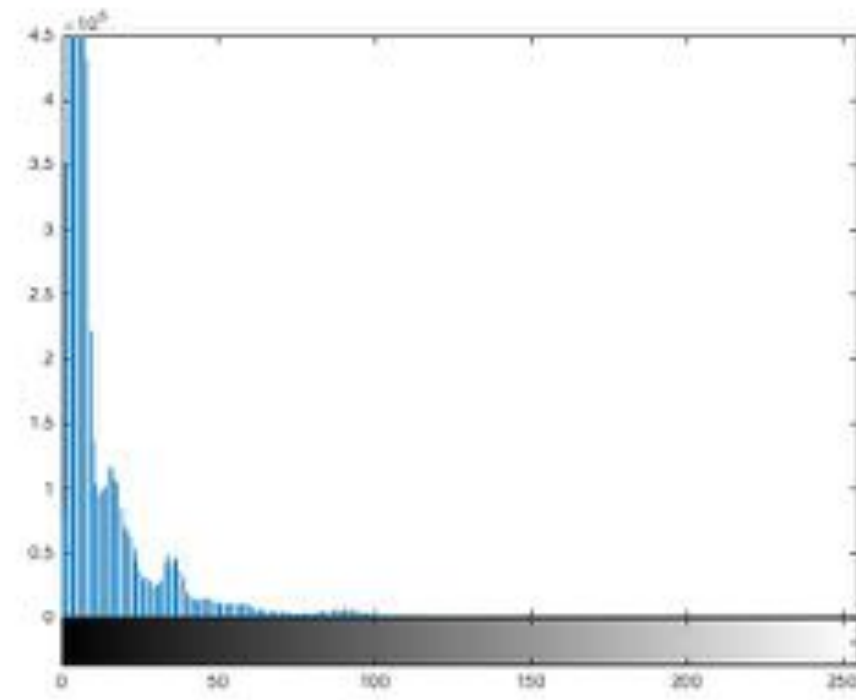
Histogram equalization



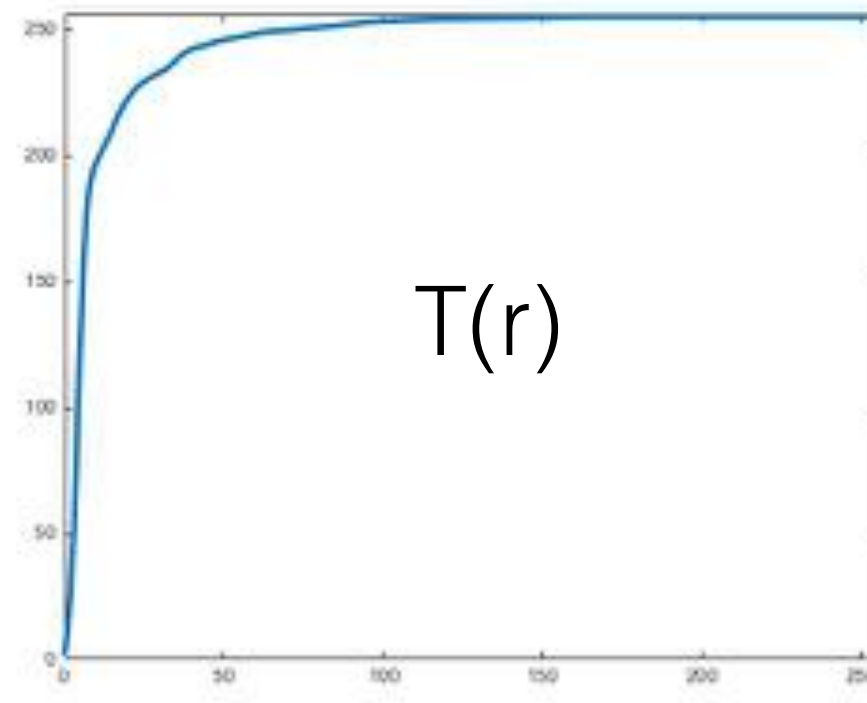
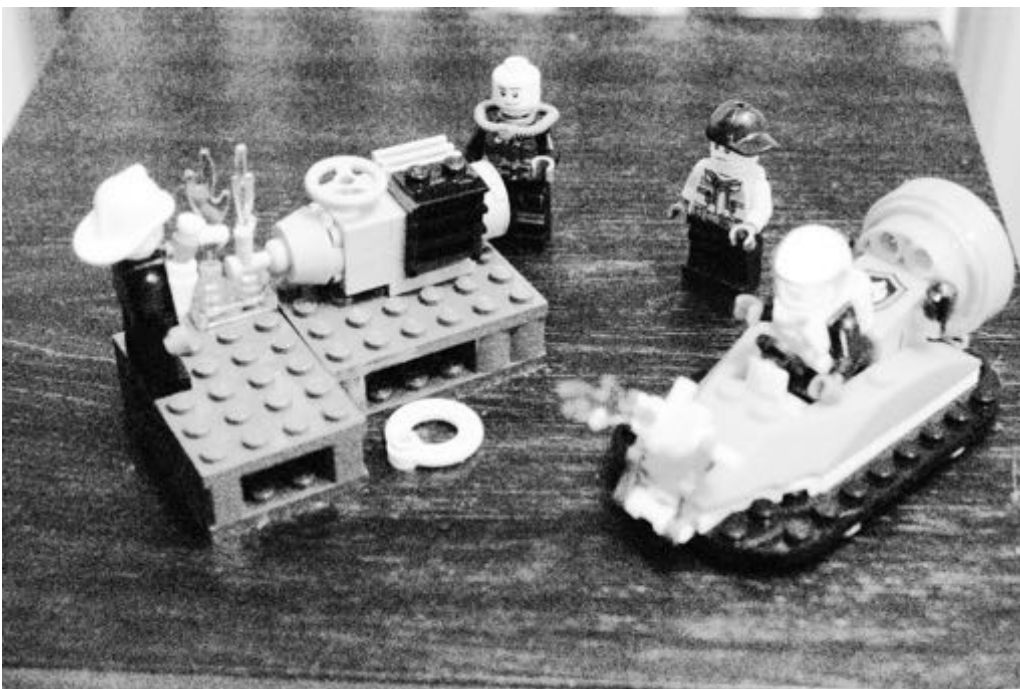
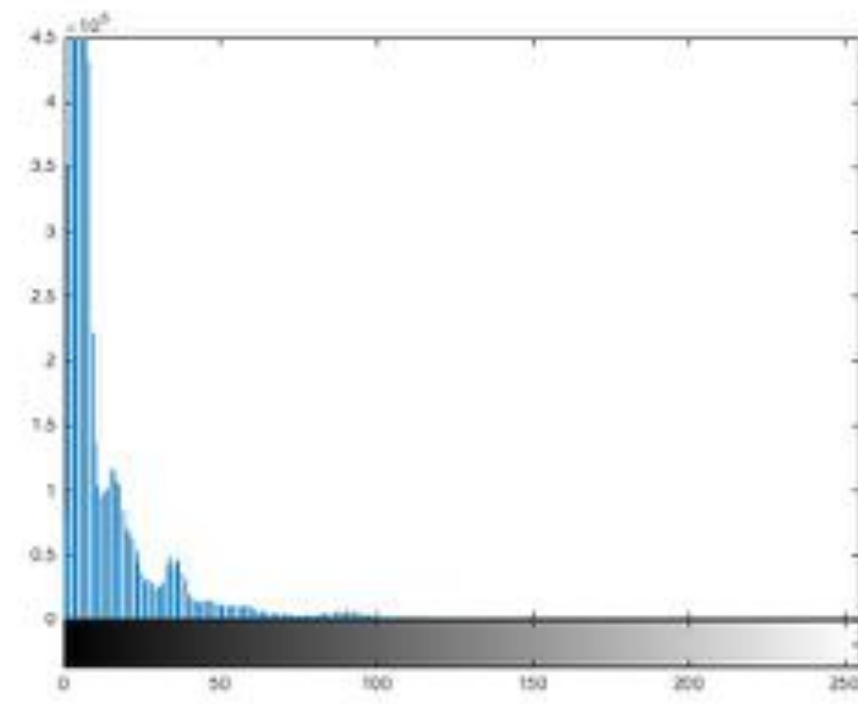
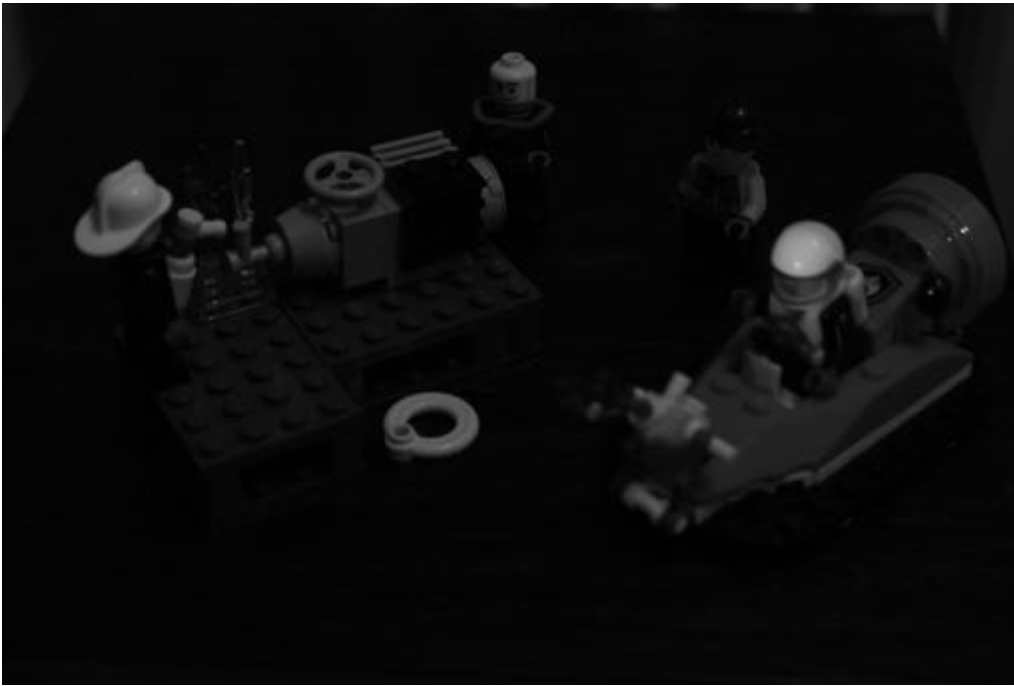
Histogram equalization



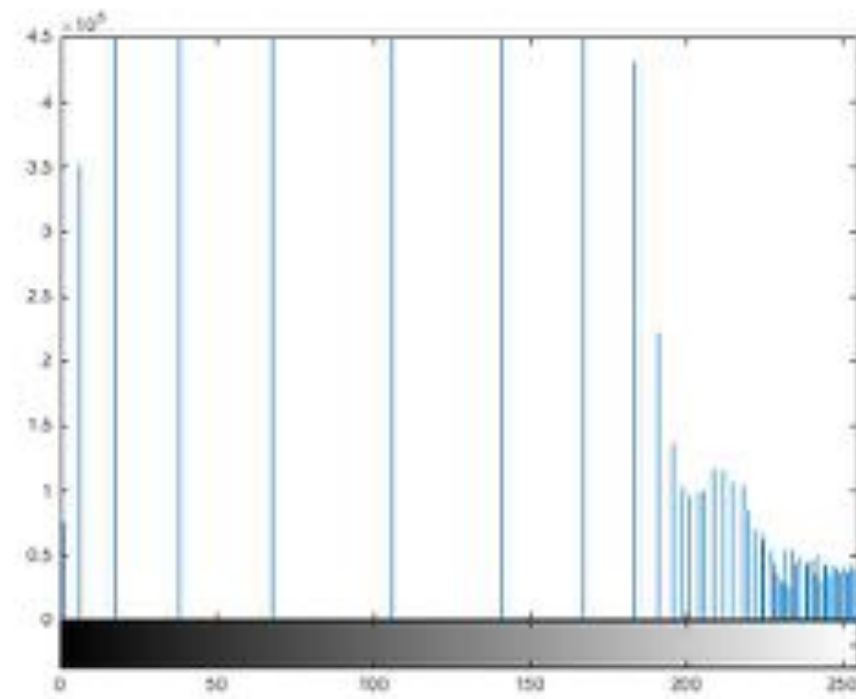
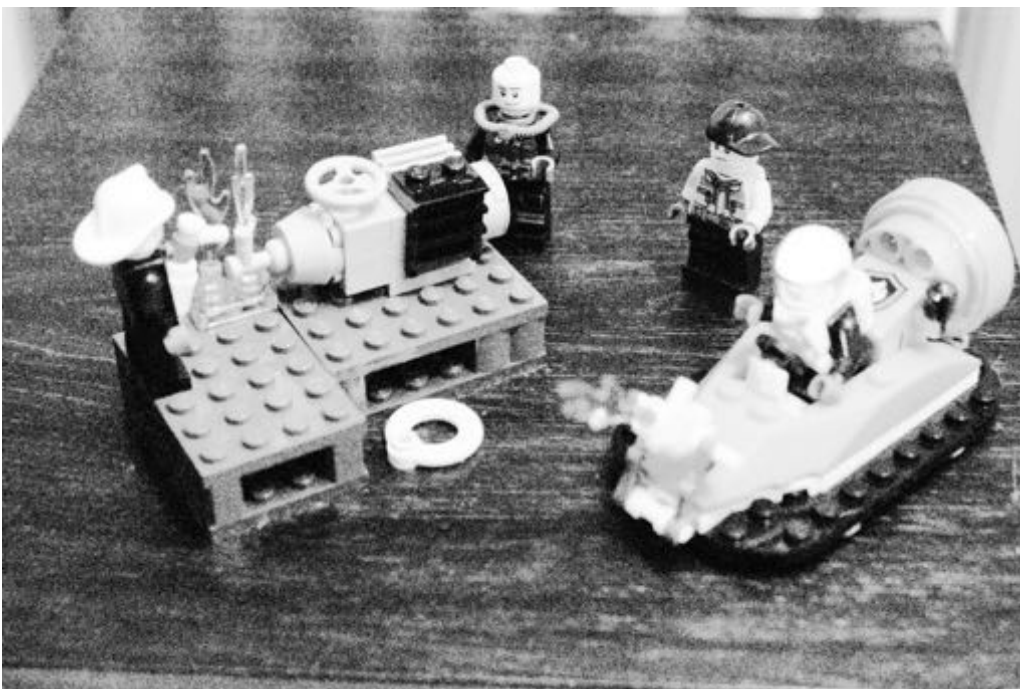
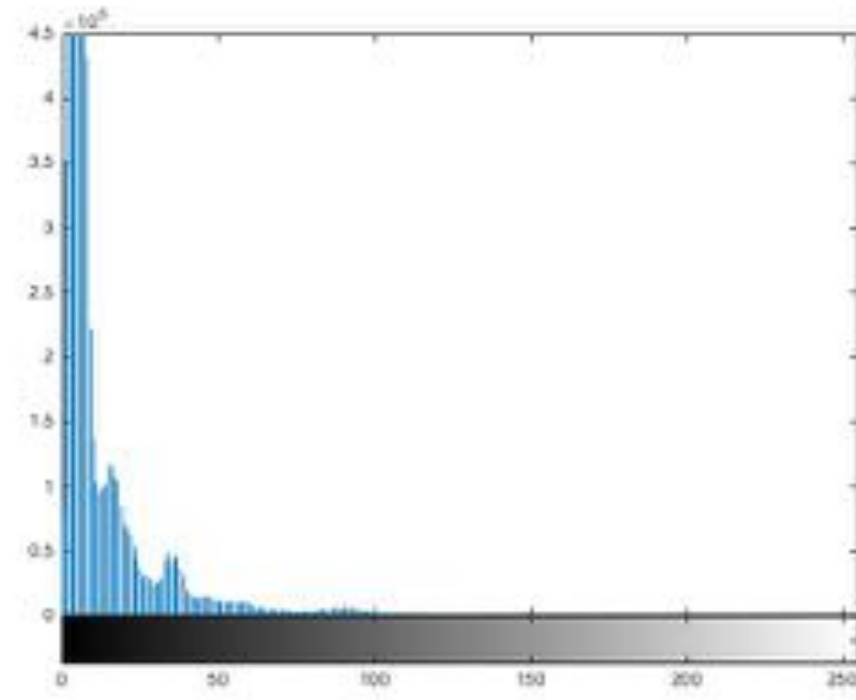
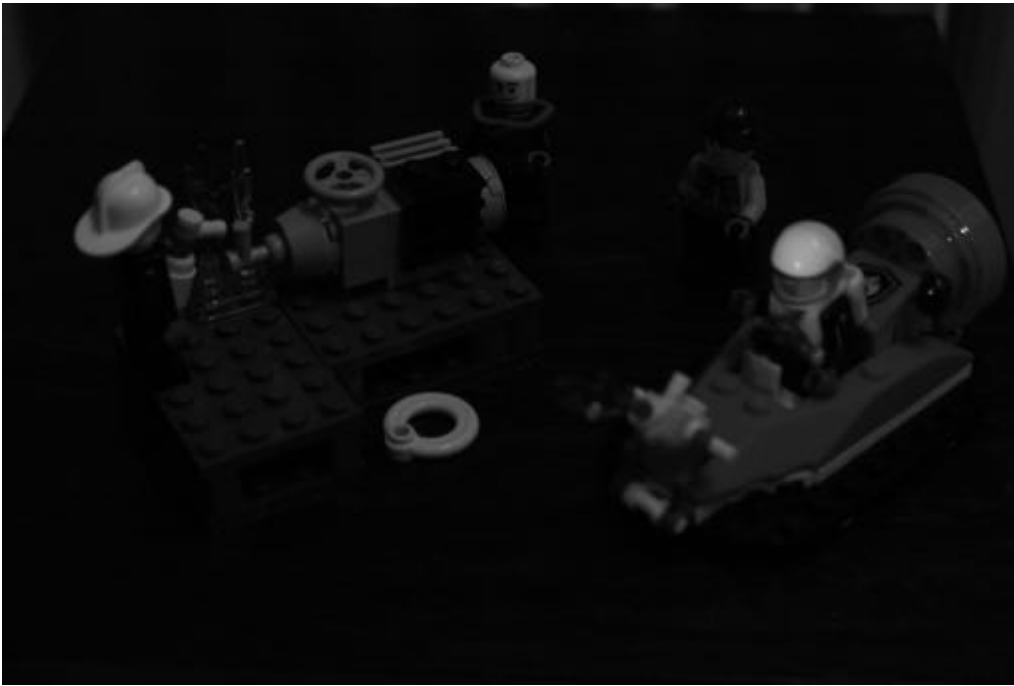
Histogram equalization



Histogram equalization



Histogram equalization



Review

- What is image analysis
- Image models
- Sampling and Interpolation
- Discrete Geometry and 'bwlabel'
- Gray-level transformations, histograms and histogram equalization
- Read lecture notes
- Experiment with matlab demo scripts
- Start working on assignment 1

Master's Thesis Suggestion of the day

- Make a system that takes inventory of a bookshelf
- I want a drone that takes inventory every night and an app that can be used to search for the right book. The drone should fly and point at the right book, when I ask for it. Voice interface.
- Help the professor. Where is my book?





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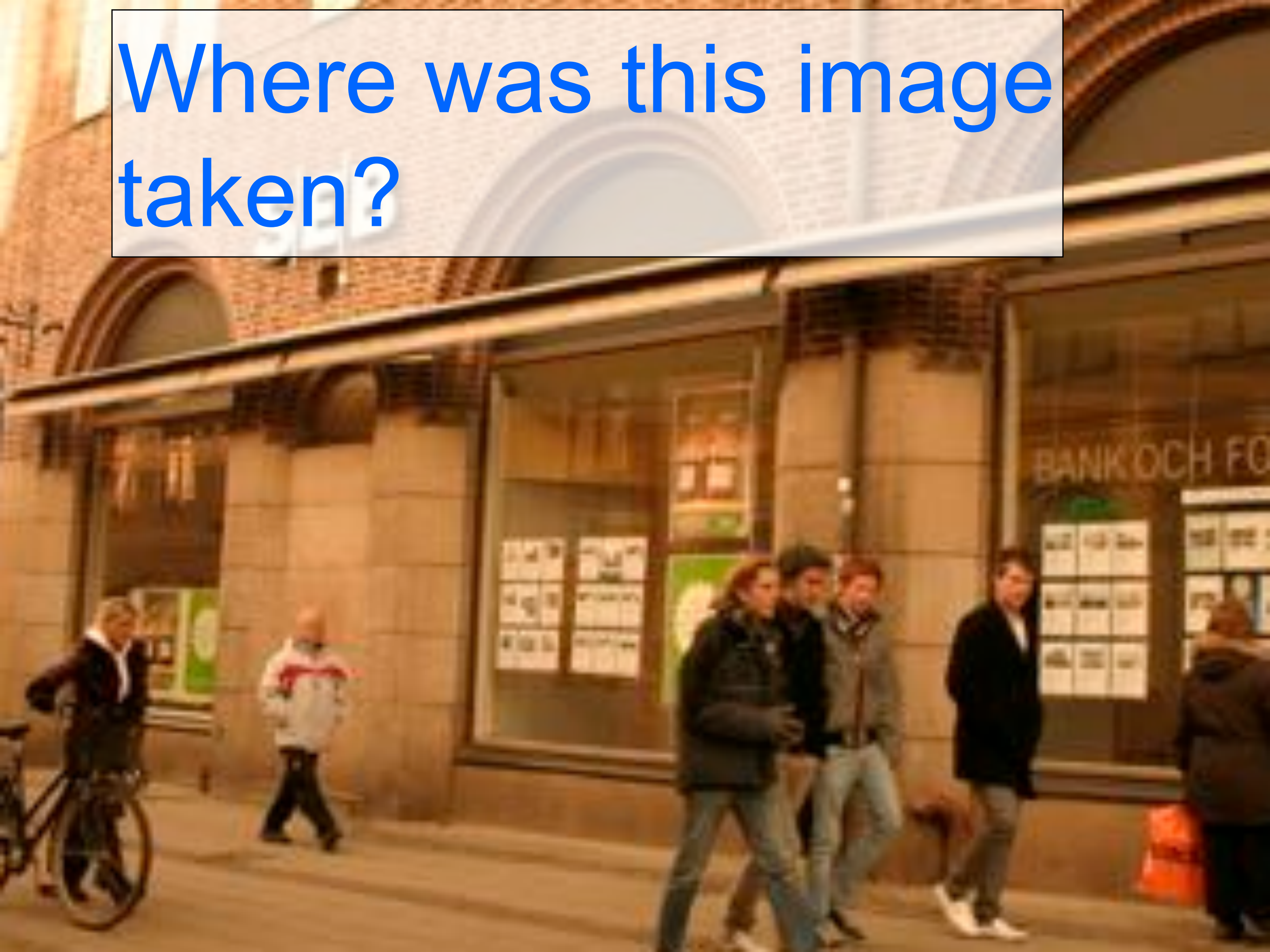


Other uses of Image Analysis in Applications

Collaborations

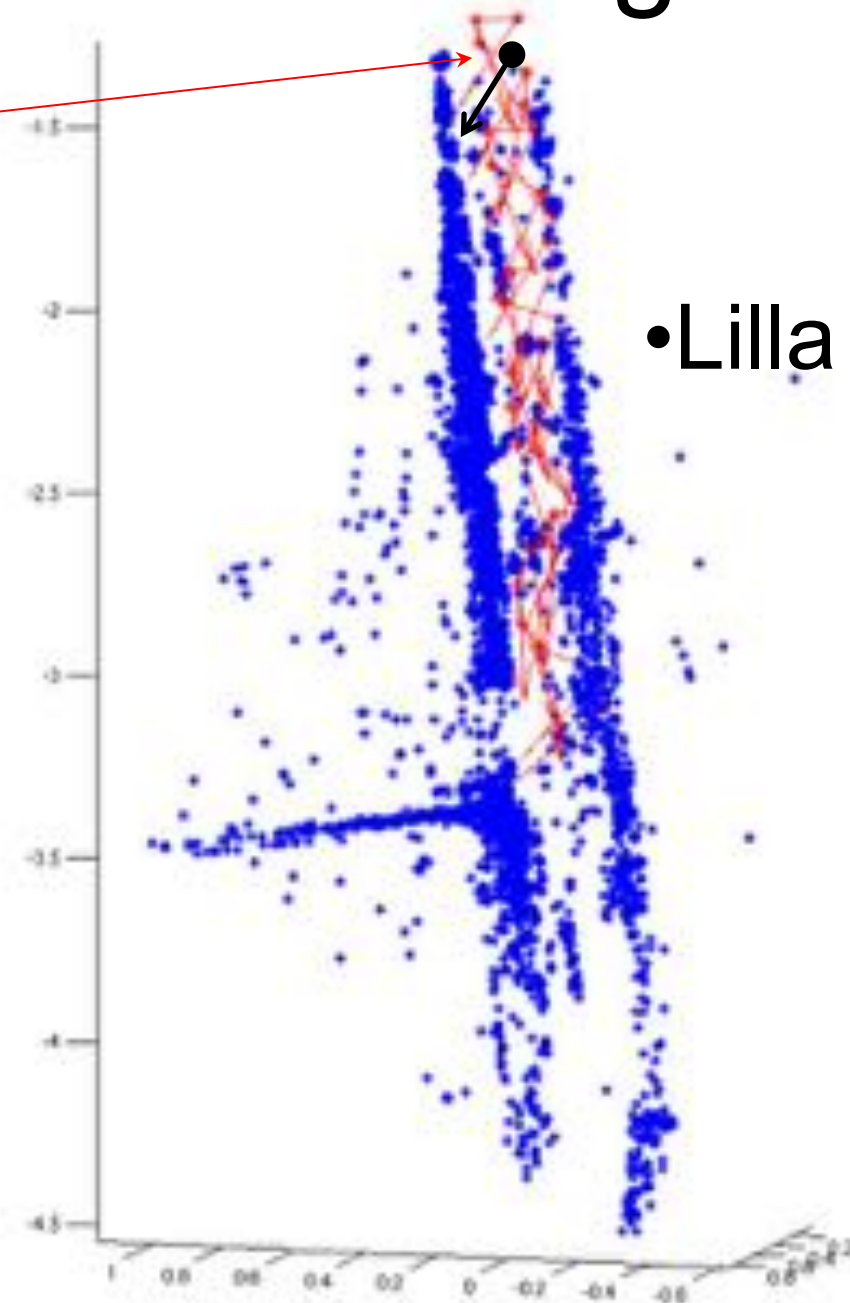
- Automatic control
- Robotics
- Traffic safety analysis
- MR
- Orthopaedics
- Radiology
- Cancer research
- Computer Science
- EIT
- Architecture
- Food (Livsmedelsteknik)
- SLU
- ...
- Sony
- Ericsson
- Axis
- Precise Biometrics
- Cellavision
- Anoto
- Exini
- Apple
- Google
- Danaher motion
- Cognimatics
- Decuma
- Polar Rose
- Spiideo
- Nocturnal Vision
- ...

Where was this image taken?



- Where was this image taken?

- Stortorget



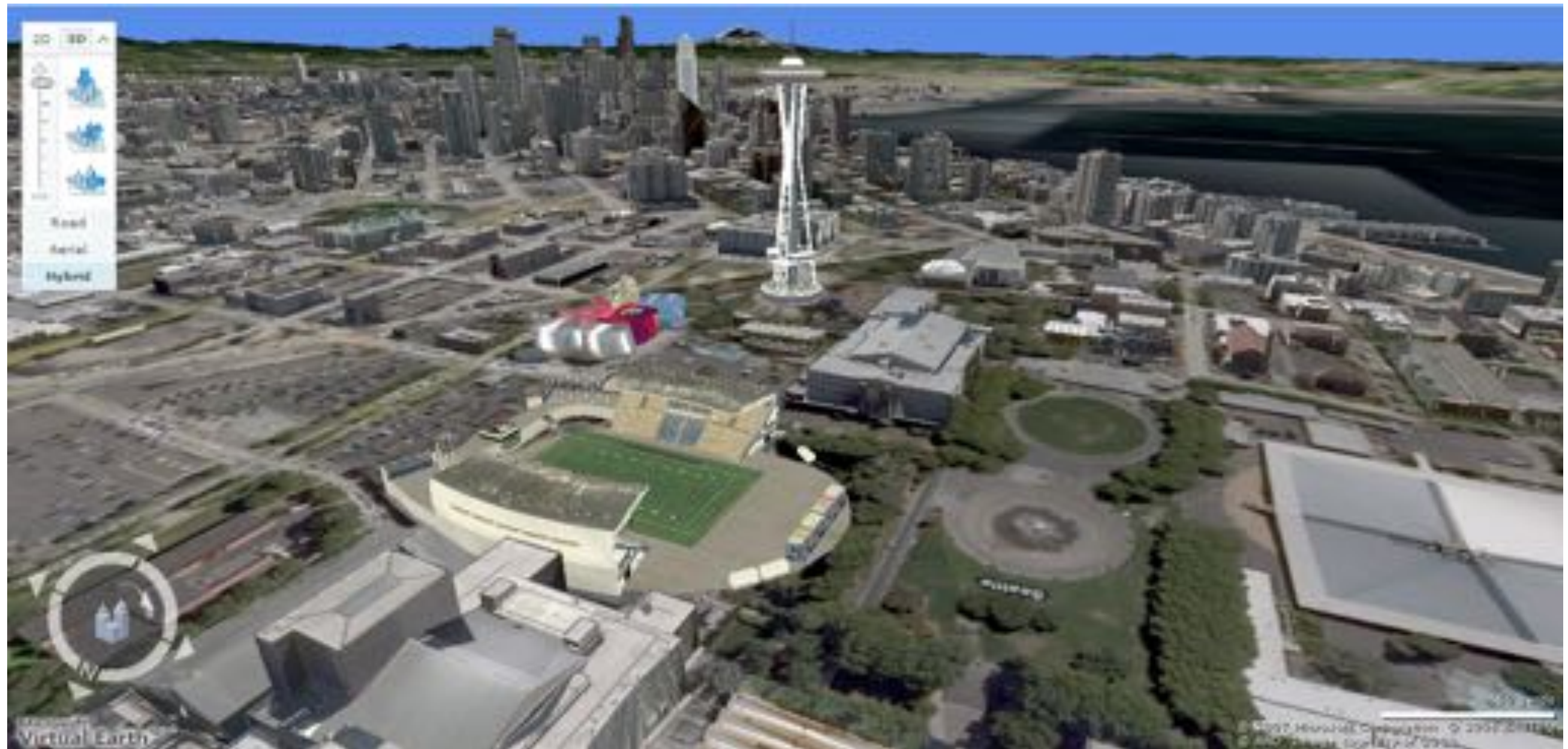
- Lilla Fiskaregatan

Object recognition (in mobile phones)



- This is becoming real:
 - **Lincoln** Microsoft Research
 - Point & Find, Nokia
 - SnapTell.com (now amazon)

Earth viewers (3D modeling)



- Image from Microsoft's [Virtual Earth](#)
- (see also: [Google Earth](#))

Face detection



- Many new digital cameras now detect faces
 - Canon, Sony, Fuji, ...

Smile detection?

The Smile Shutter flow

Imagine a camera smart enough to catch every smile! In Smile Shutter Mode, your Cyber-shot® camera can automatically trip the shutter at just the right instant to catch the perfect expression.

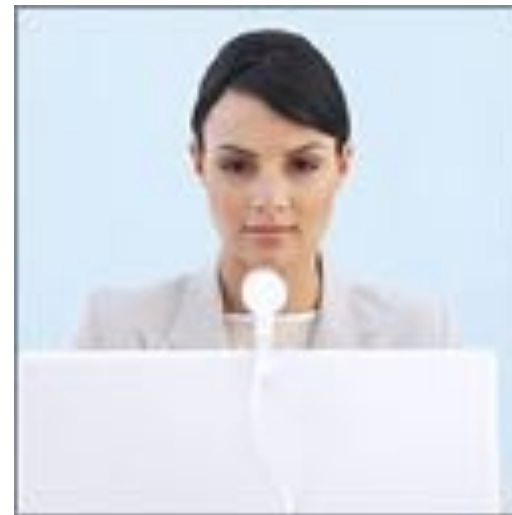


- [Sony Cyber-shot® T70 Digital Still Camera](#)

Login without a password...



- Fingerprint scanners on many new laptops, other devices



- Face recognition systems now beginning to appear more widely
<http://www.sensiblevision.com/>

Special effects: shape capture



- *The Matrix* movies, ESC Entertainment, XYZRGB, NRC

Special effects: motion capture



- *Pirates of the Caribbean*, Industrial Light and Magic
- [Click here for interactive demo](#)

Sports



- *Sportvision* first down line
- Nice [explanation](http://www.howstuffworks.com) on www.howstuffworks.com

Smart cars



- [Mobileye](#)

- Vision systems currently in high-end BMW, GM, Volvo models
- By 2010: 70% of car manufacturers.
- [Video demo](#)

• Slide content courtesy of Amnon Shashua

Smart cars

The screenshot displays the Mobileye website interface. At the top, there are navigation tabs for 'manufacturer products' and 'consumer products'. The main headline reads 'Our Vision. Your Safety.' Below this, a 3D rendering of a car is shown with three camera fields of view highlighted: 'rear looking camera', 'side looking camera', and 'forward looking camera'. To the right, a 'News' sidebar lists articles such as 'mobileye advanced Technologies Power Volvo Cars World First Collision Warning With Auto Brake System' and 'Volvo's New Collision Warning with Auto Brake Helps Prevent Rear-end'. Below the main car image, there are three sections: 'EyeQ Vision on a Chip' with an image of a chip, 'Vision Applications' showing a pedestrian crossing, and 'AWS Advance Warning System' with a car icon. At the bottom right, a video player shows a road scene with a car detected by a green box and a distance of '56.1m' displayed. The video player has a timestamp of '8:0014' and '8:05'.

- [Mobileye](#)

- Vision systems currently in high-end BMW,
- By 2010: 70% of car manufacturers.

- [Video demo](#)

• Slide content courtesy of Amnon Shashua

Vision-based interaction (and games)



- [Digimask](#): put your face on a 3D avatar.

- Nintendo Wii has camera-based IR tracking built in. See [Lee's work at CMU](#) on clever tricks on using it to create a [multi-touch display](#)!



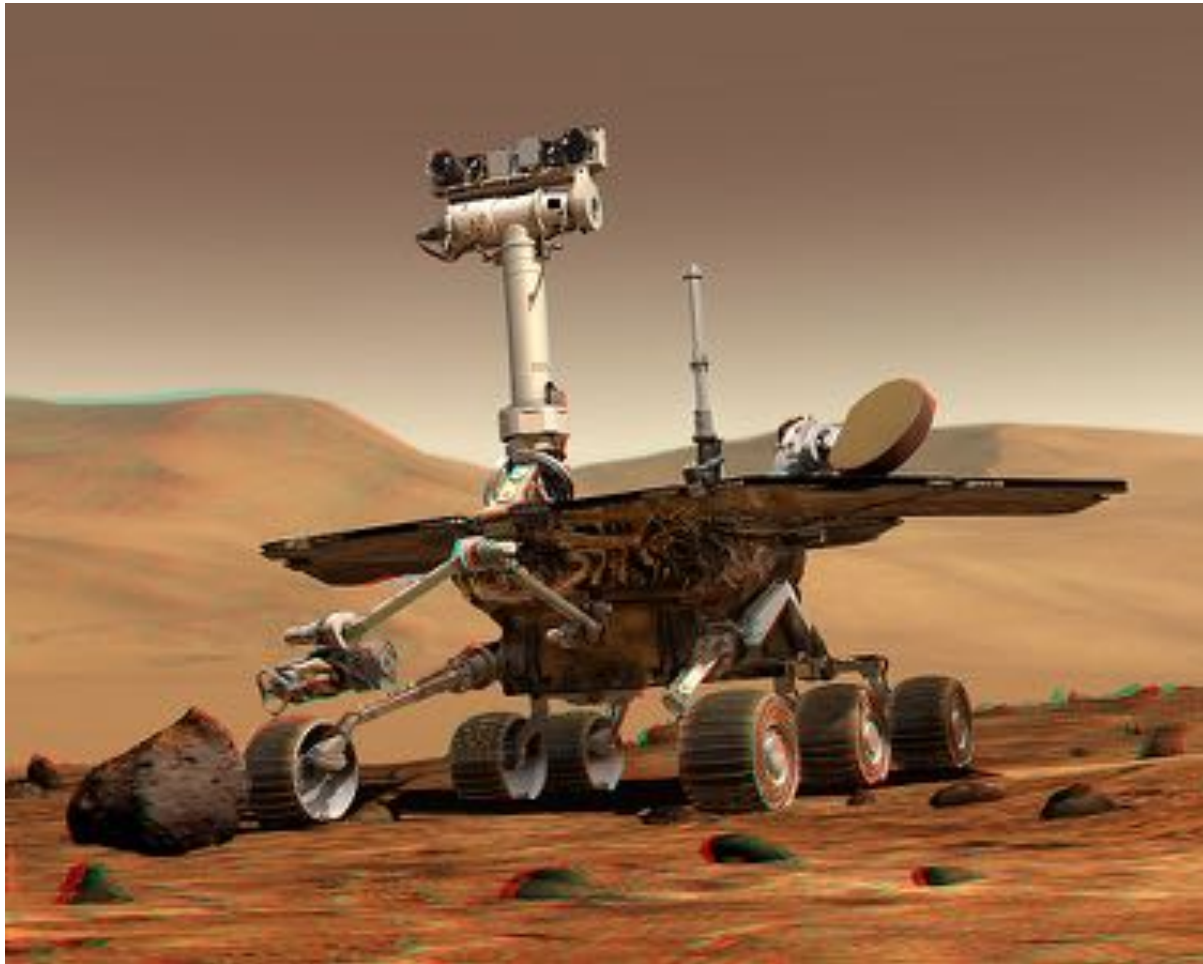
- [“Game turns moviegoers into Human Joysticks”](#), CNET
 - Camera tracking a crowd, based on [this work](#).

Vision in space



- [NASA'S Mars Exploration Rover Spirit](#) captured this westward view from atop a low plateau where Spirit spent the closing months of 2007.
- Vision systems (JPL) used for several tasks
 - Panorama stitching
 - 3D terrain modeling
 - Obstacle detection, position tracking
- For more, read “[Computer Vision on Mars](#)” by Matthies et al.

Robotics

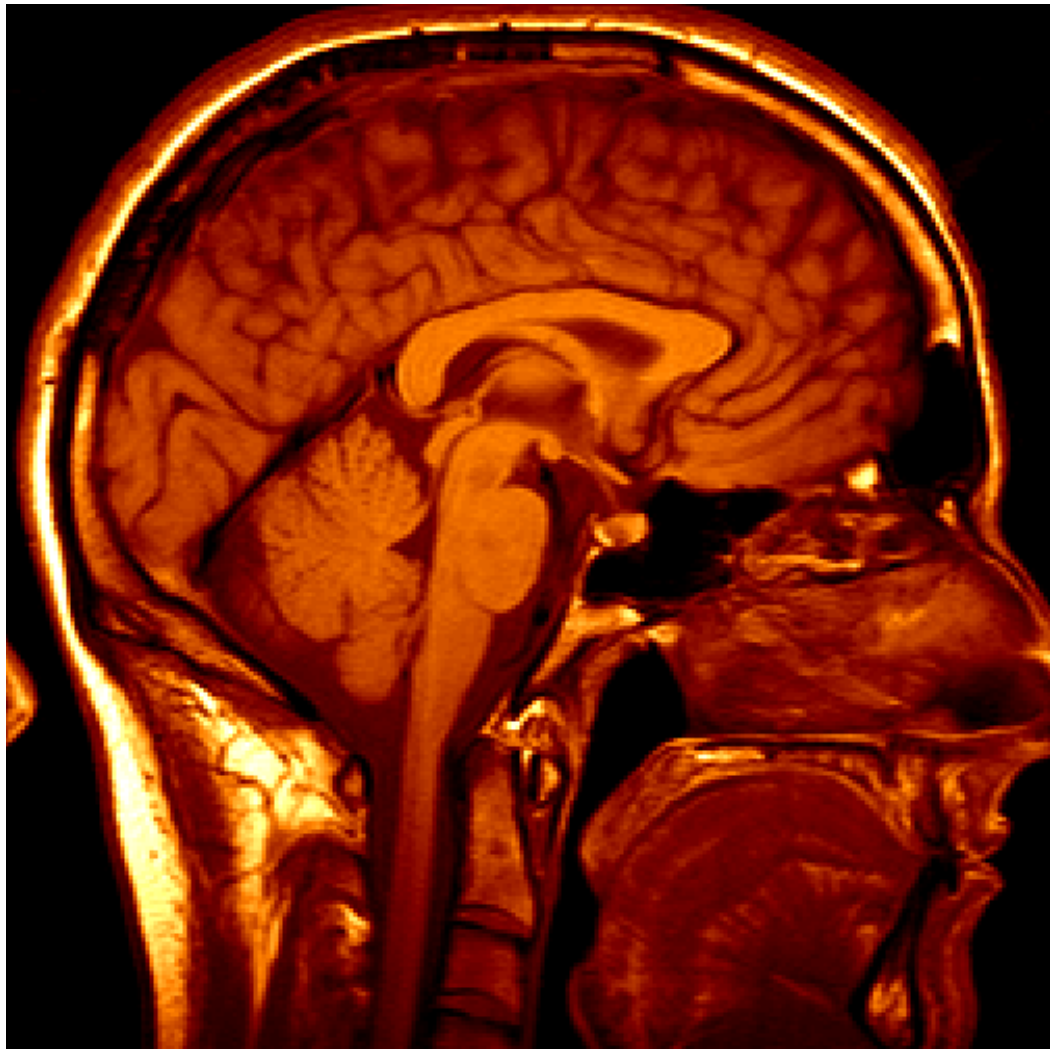


- NASA's Mars Spirit Rover
- http://en.wikipedia.org/wiki/Spirit_rover



- <http://www.robocup.org/>

Medical imaging



- 3D imaging
- MRI, CT



- Image guided surgery
- [Grimson et al., MIT](#)